

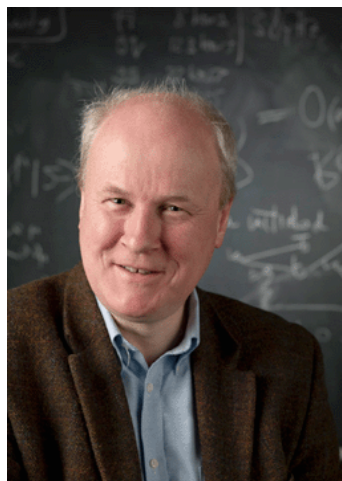
Constraining Higgs boson properties using MCFM

EPP Seminar, U. Penn, 17 March 2015
John Campbell

MCFM

- ★ **MCFM = Monte Carlo for FeMtobarn** processes: <http://mcfm.fnal.gov>
- ★ A parton-level Monte Carlo program that provides next-to-leading order predictions for a variety of Standard Model processes.

K. Ellis
(FNAL)



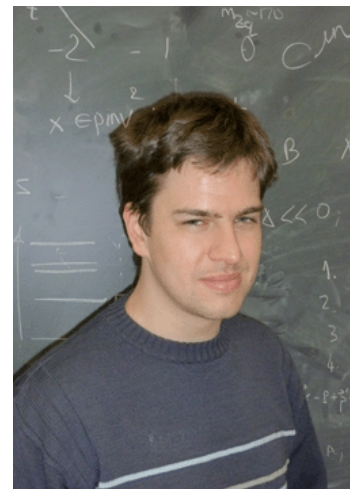
C. Williams
(Buffalo)



W. Giele
(FNAL)



R. Röntsch
(FNAL)

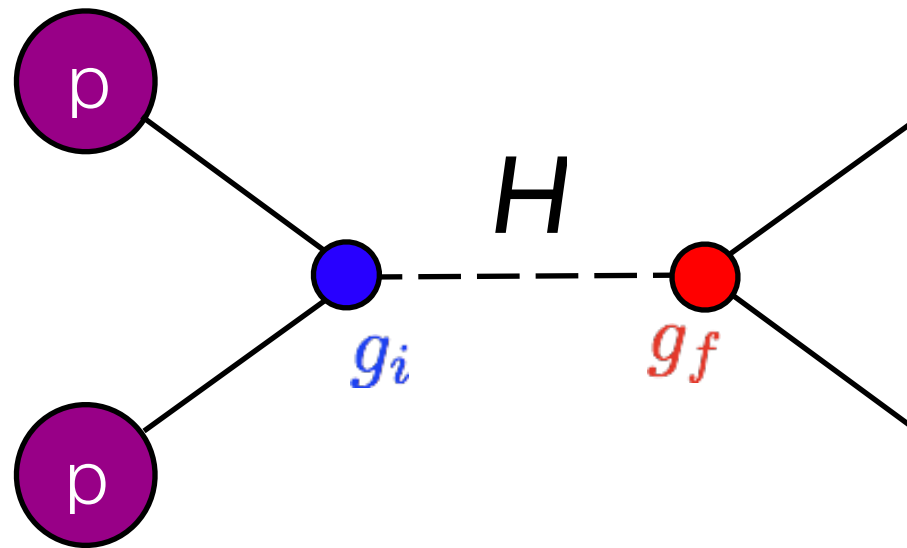


- ★ In this talk I will focus on developments in recent years aimed at helping to characterize Higgs boson properties: width and couplings to W and Z.

arXiv: 1311.3589, 1312.1628, 1409.1897, 1502.02990

Cross sections to parameters

- ★ Key question: how to go from measurements to parameters in the Lagrangian.
- ★ First pass, appropriate for data collected so far, simple parametrization that just scales SM couplings.



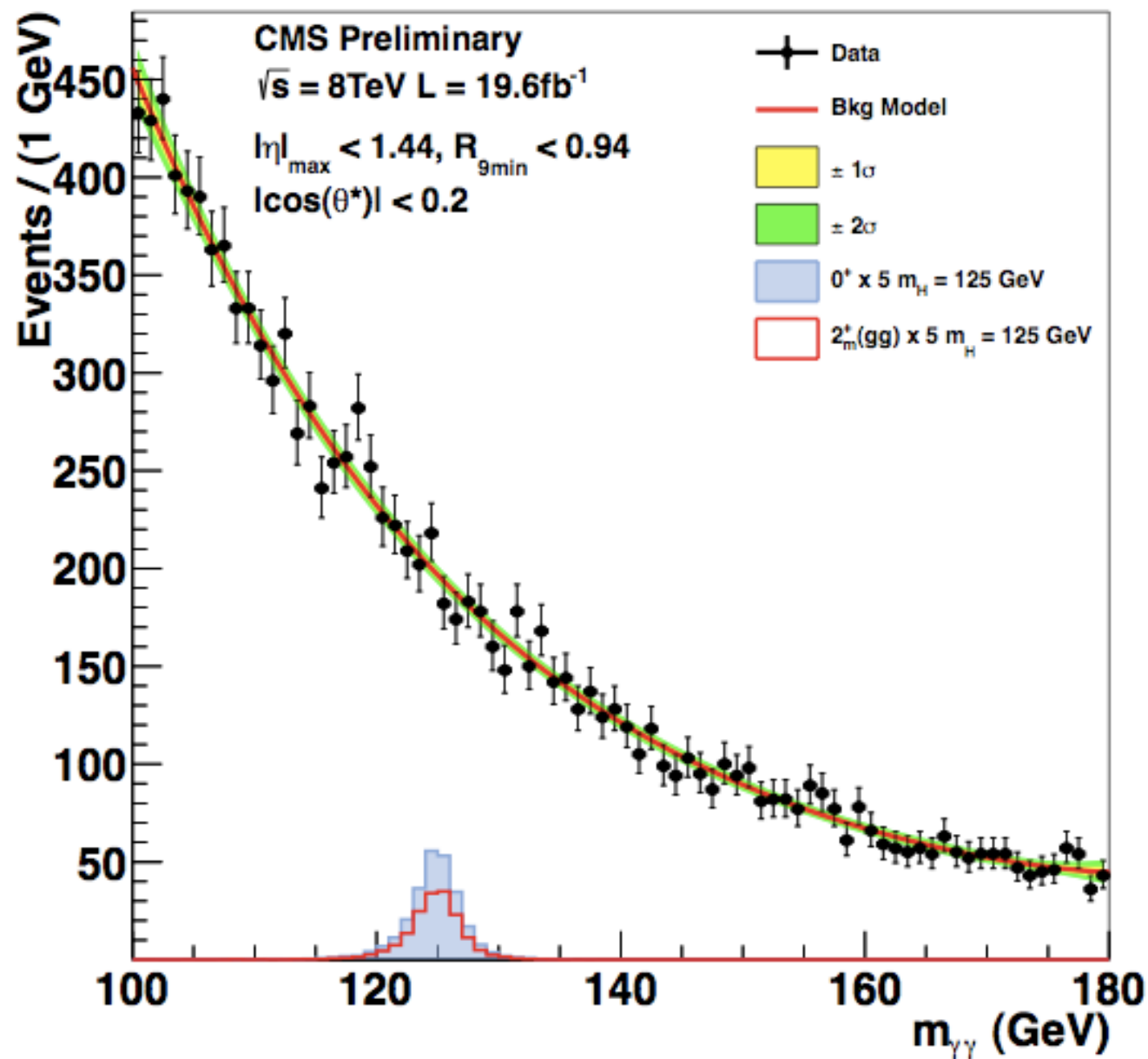
- ★ Total cross section depends on the strengths of the couplings of the Higgs boson in its initial production and final decay stages g_i and g_f and also on the width:

$$\sigma_{i \rightarrow H \rightarrow f} \sim \frac{g_i^2 g_f^2}{\Gamma_H}$$

- ★ How can these be disentangled to avoid degeneracy? Can width be probed?

Direct width constraints

- ★ How can we probe a SM width of 4 MeV at the LHC?



CMS PAS HIG-13-016

- Intrinsic detector resolution is of order a few GeV in the most well-measured channels.

- Limits inherently weak, e.g. CMS:

$$\Gamma_H < 6.9 \text{ GeV}$$

(95% confidence)

$$(\Gamma_H \lesssim 1600 \Gamma_H^{\text{SM}})$$

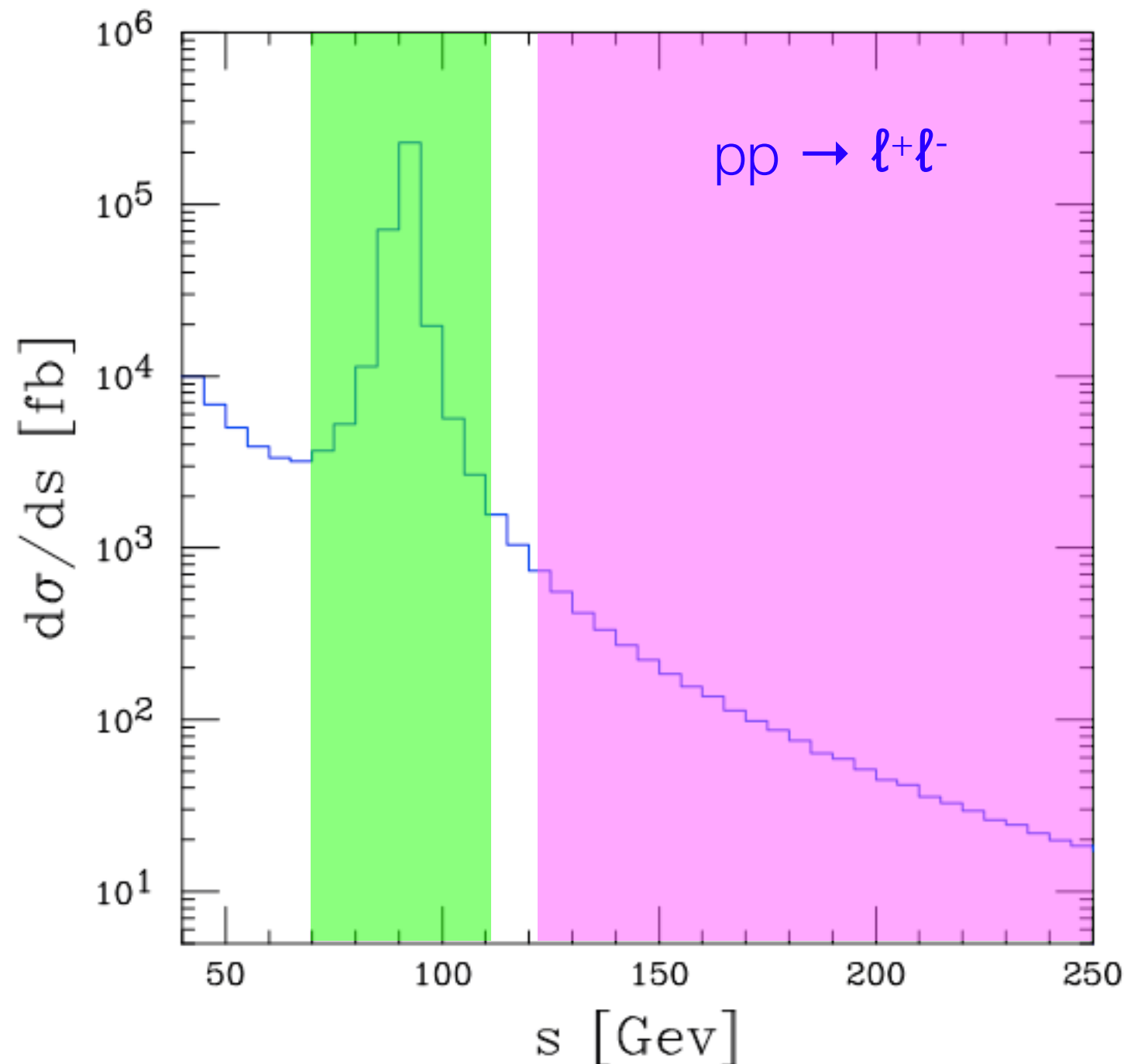
- Assume bound scales with statistics, combine with ZZ channel, 3000 fb⁻¹:

$$\Gamma_H \lesssim 200 \text{ MeV} \quad (\sim 50 \Gamma_H^{\text{SM}})$$

The Caola-Melnikov method

(essence of 1307.4935)

- ★ Consider the Drell-Yan process. Can map out the resonance as a function of the four-momentum squared (s) that appears in the propagator.



- ▶ “On-shell” cross section in resonance region:

$$\sigma_{\text{on}} \sim \int \frac{ds}{(s - m_Z^2)^2 + \Gamma_Z^2 m_Z^2} \propto \frac{1}{\Gamma_Z}$$

- ▶ “Off-shell” cross section above the resonance:

$$\sigma_{\text{off}} \sim \int_{s \gg m_Z^2} \frac{ds}{(s - m_Z^2)^2 + \Gamma_Z^2 m_Z^2}$$

(approx.) independent of width.

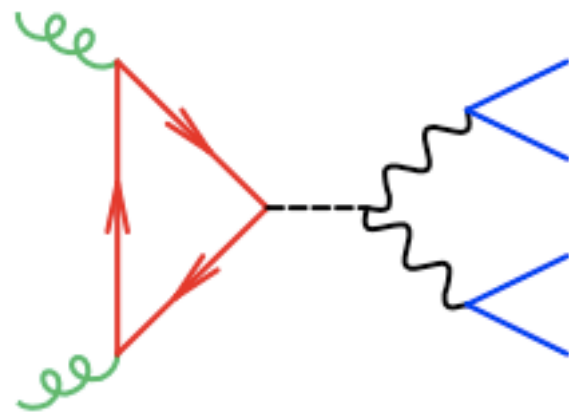
$$\Gamma \propto \frac{\sigma_{\text{off}}}{\sigma_{\text{on}}}$$

The Higgs golden channel

- ★ Naive expectation: $\Gamma_H/m_H \sim 10^{-5}$; resonance peak so narrow that there is no off-shell cross section to measure.
- ★ This is spectacularly wrong for the golden channel.

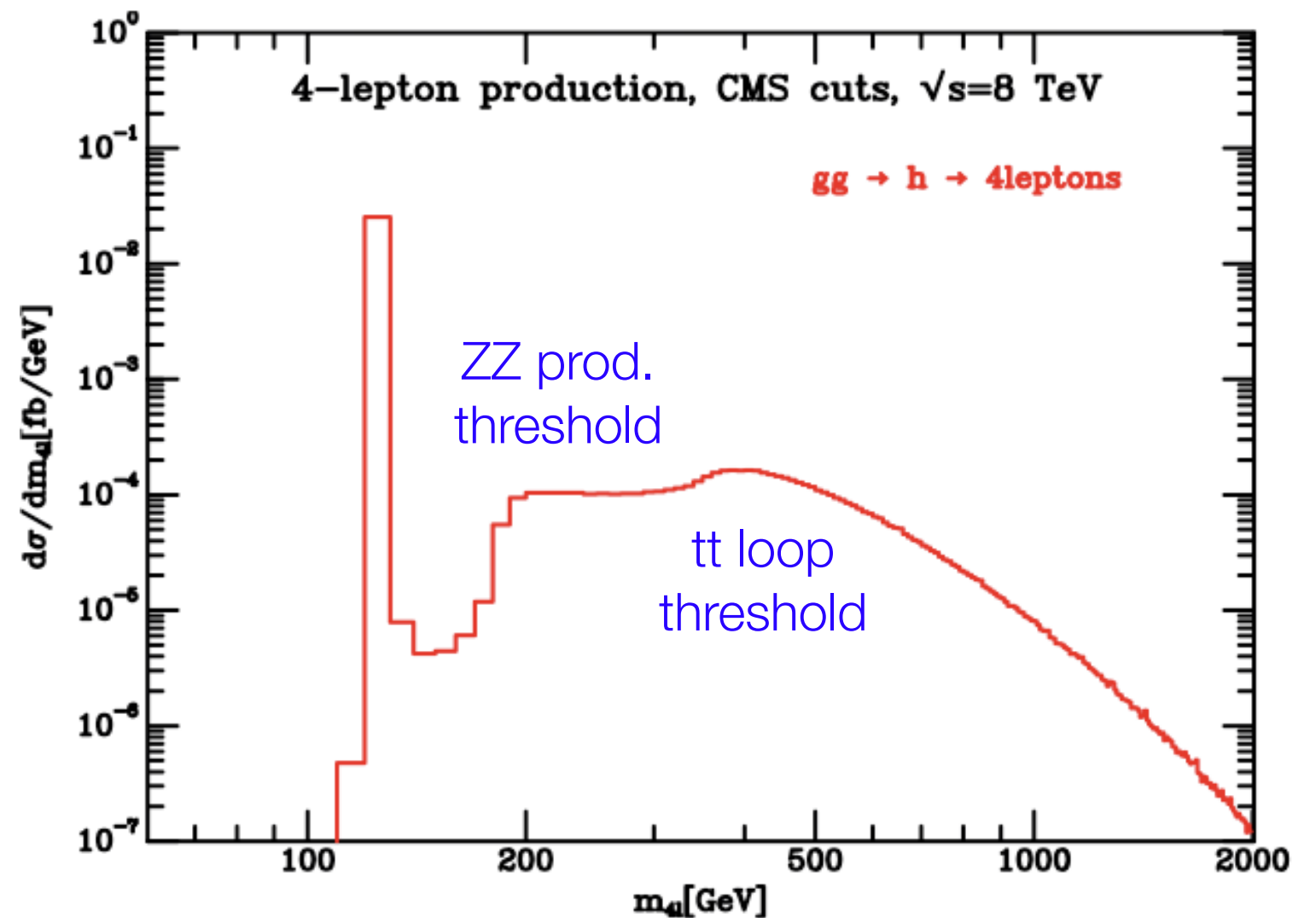
$$p + p \rightarrow H \rightarrow ZZ$$

$$\begin{array}{l} \searrow \rightarrow \mu^- + \mu^+ \\ \searrow \rightarrow e^- + e^+ \end{array}$$



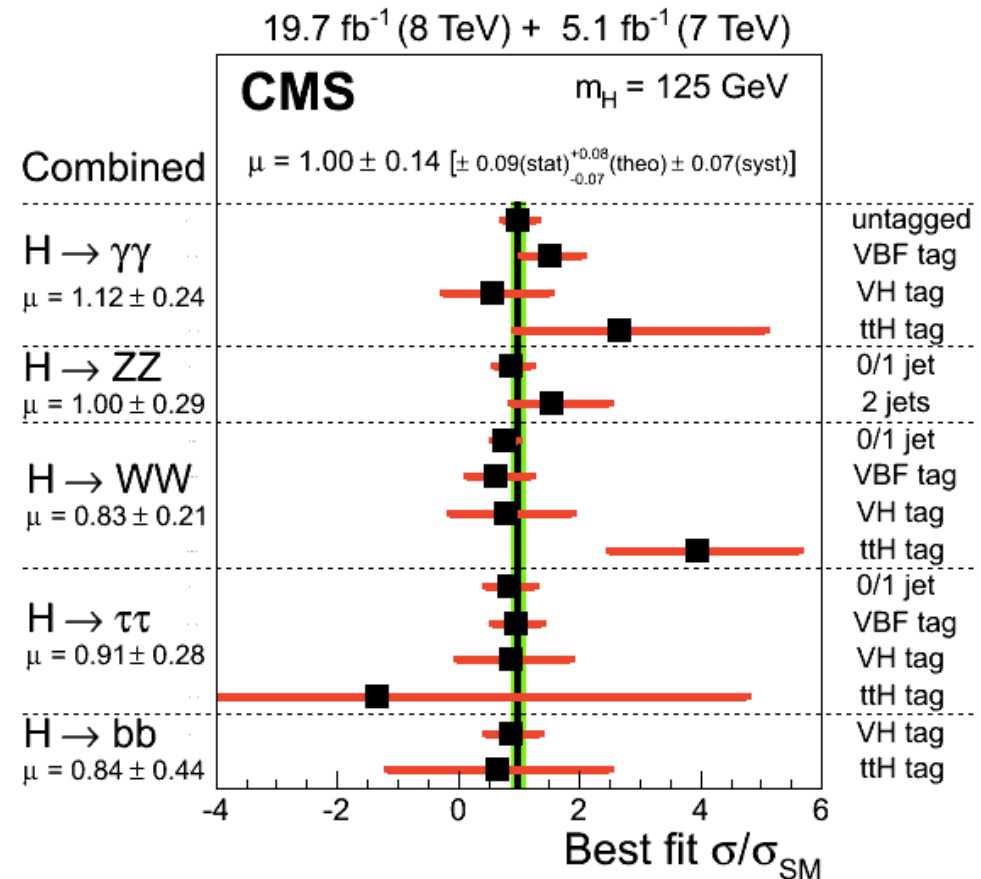
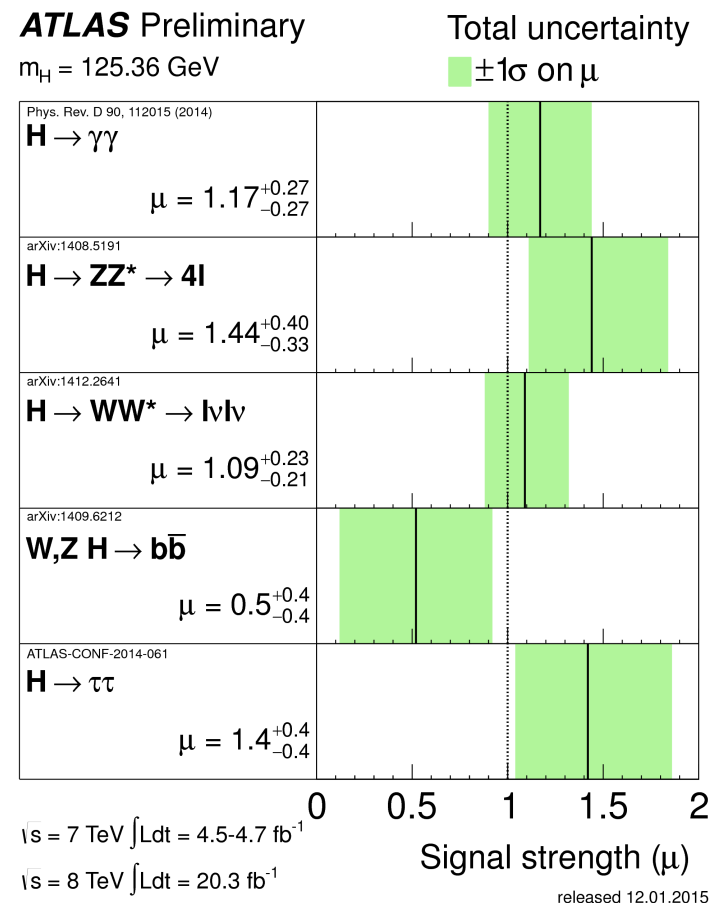
- ★ About 15% of the total cross section lies in the region with $m_{4\ell} > 130$ GeV.

Kauer, Passarino, 1206.4803



Strategy

- ★ We know that the peak cross-section is in good agreement with SM expectation.



- ★ Fixing the on-shell cross-section to the SM value means that **a larger Higgs boson width leads to more off-shell events.**

$$\Gamma \propto \frac{\sigma_{\text{off}}}{\sigma_{\text{on}}}$$

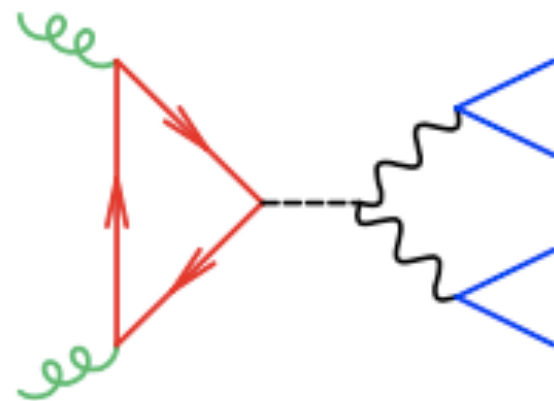
- ★ Need precise prediction for $H \rightarrow 4\text{-leptons}$ to turn measured rate into a constraint.

Calculation and results

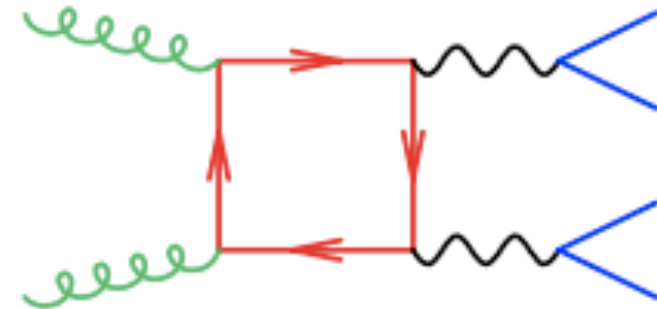
4-lepton production diagrams

- ★ Not just the Higgs boson diagrams leading to 4-lepton final state!

Higgs

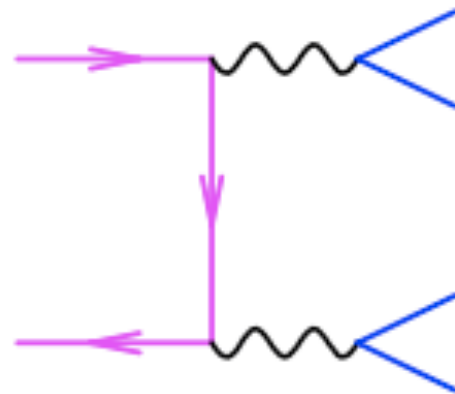


(a)



(b)

SM
background

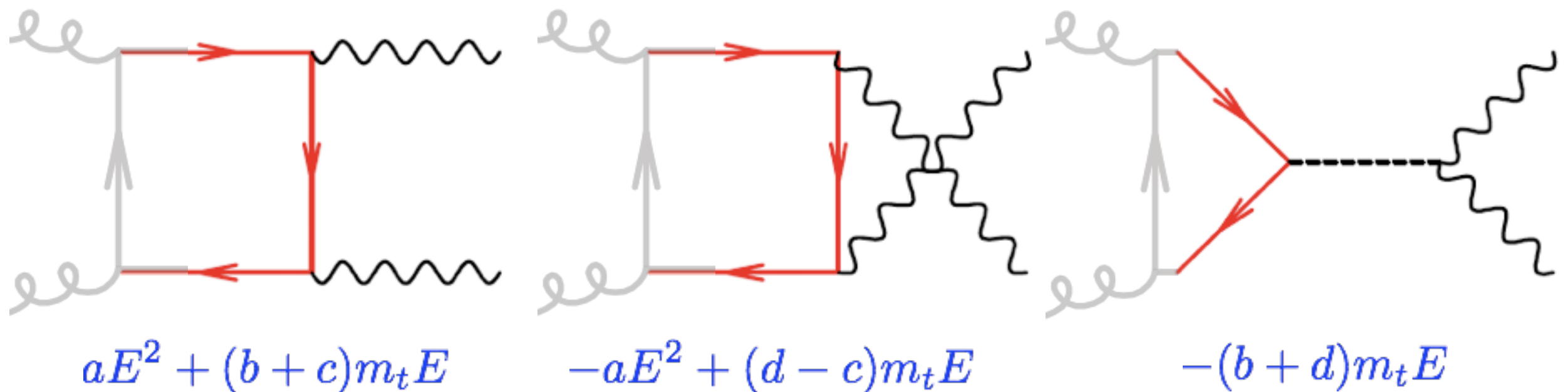


(c)

$gg \rightarrow ZZ \rightarrow 4l$
box

Importance of interference

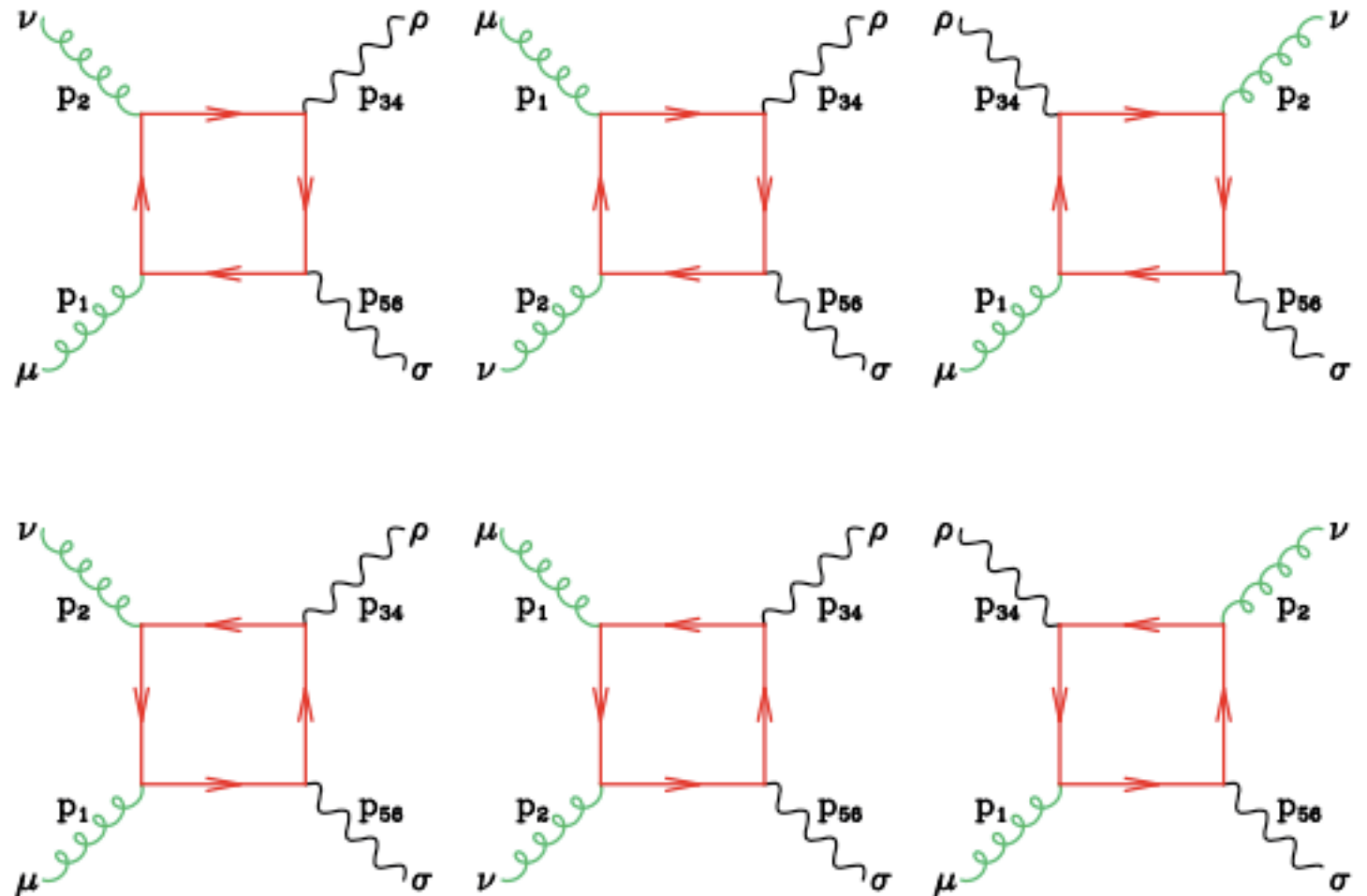
- ★ Usual classification into “signal” and “background” contributions neglects the effect of interference, which is particularly important since a Higgs boson is involved.
- ★ Consider high-energy $t\bar{t} \rightarrow ZZ$ scattering (diagrams embedded in loops), where it is straightforward to examine behavior using longitudinal modes of Z 's.



- ★ Inclusion of Higgs diagram essential to cancel bad high energy behaviour; observation of this mechanism would be evidence of the Higgs boson doing its job.
- ★ Destructive interference weakens bound: $\sigma_{\text{off}}/\sigma_{\text{on}} \approx a\Gamma - b\sqrt{\Gamma}$

Calculation

- ★ Most challenging calculation is the $gg \rightarrow ZZ$ box diagrams.
- ★ Essential to account for quark masses in the loop to obtain correct high-energy behaviour.
- ★ A long and rich history of such calculations.
- ★ Original calculation using dispersive techniques in 1971!

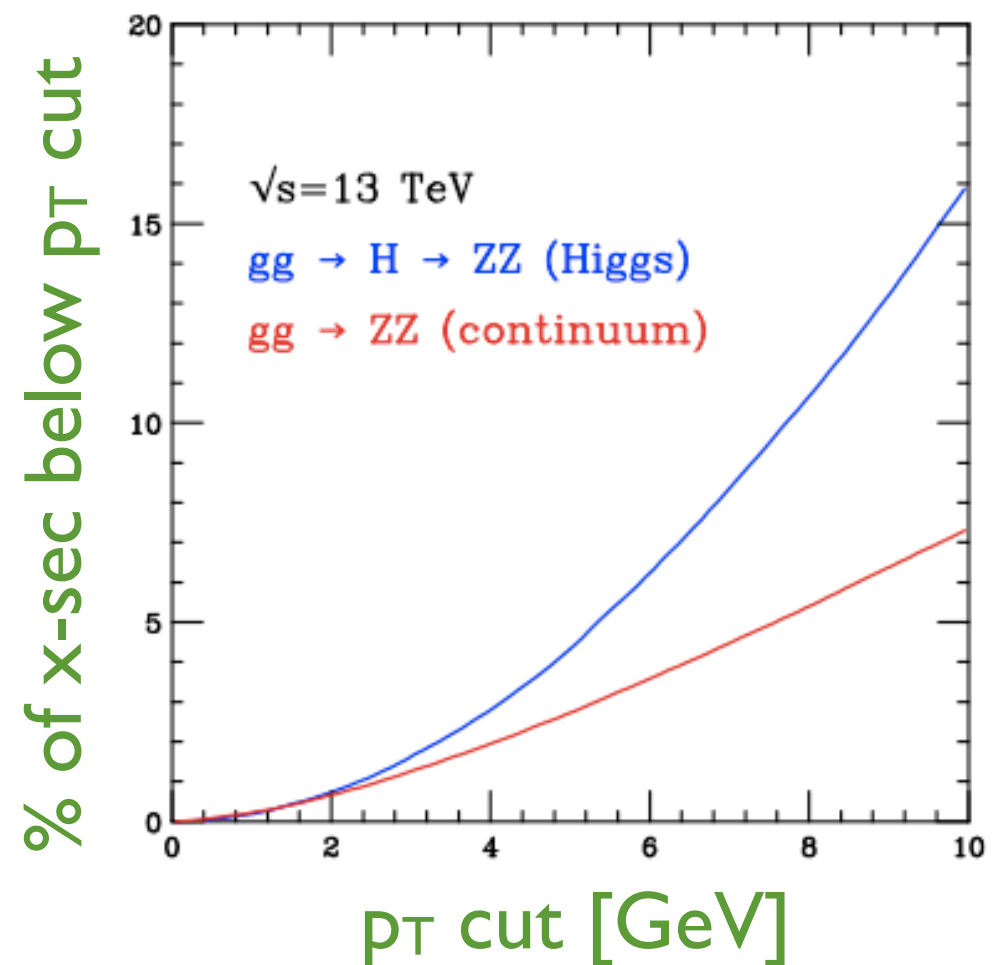
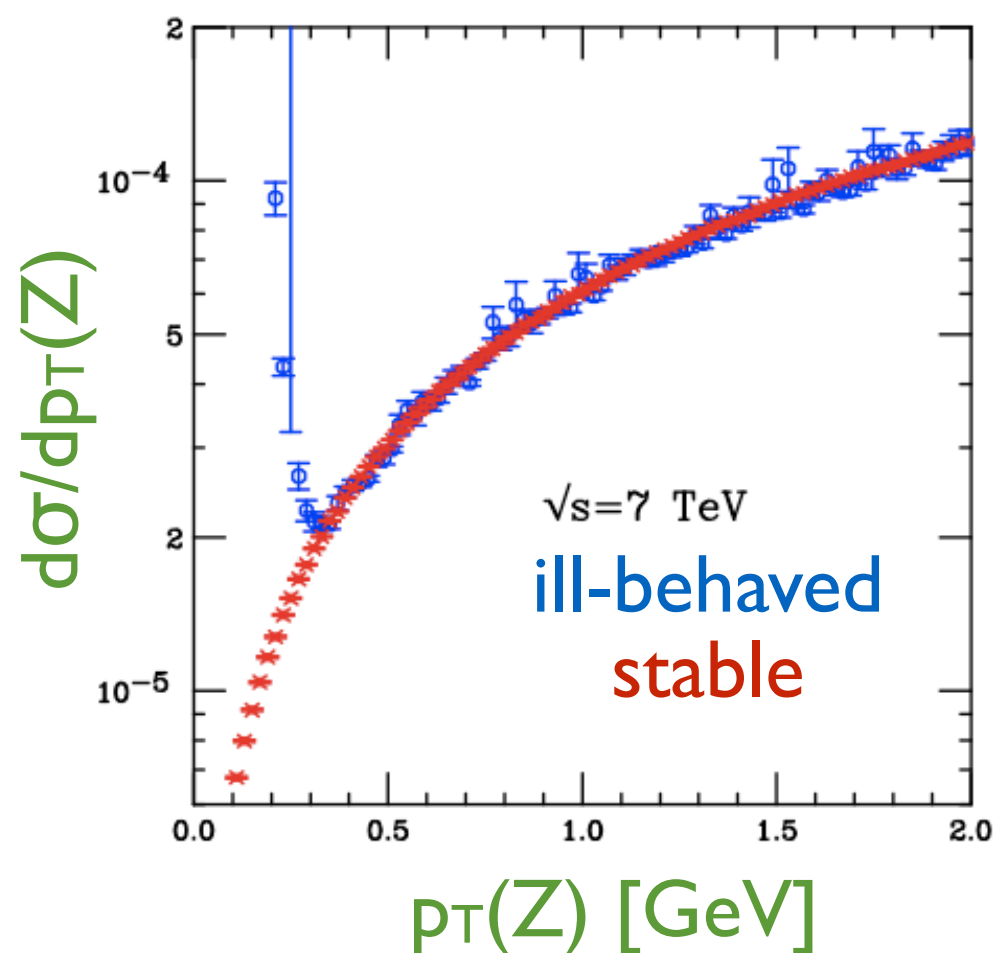


Constantini, de Tollis, Pistoni; Nuovo Cim. A2 (1971)

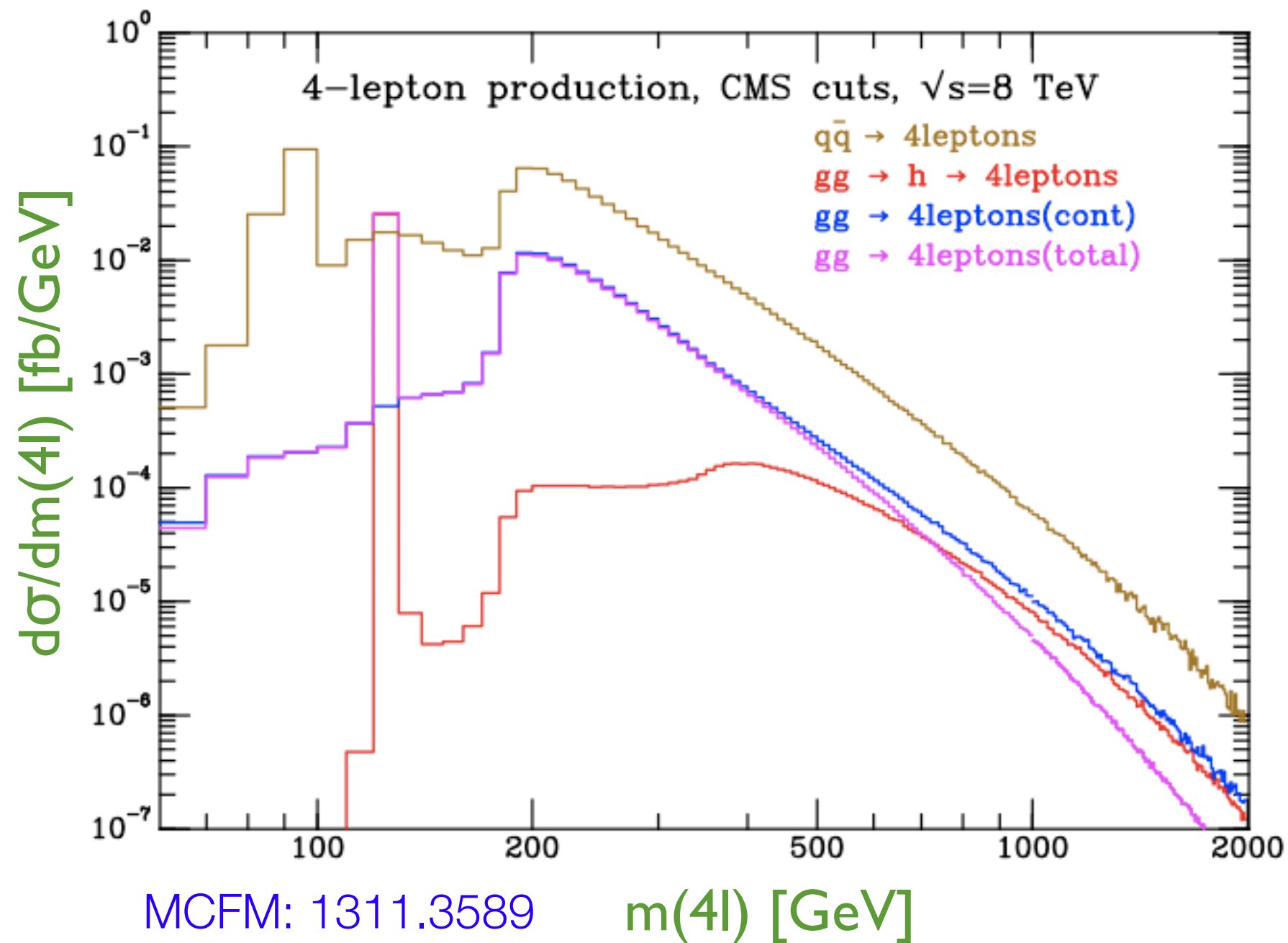
- ★ More recently, implementation of all contributions numerically in gg2VV code.
Kauer, Passarino; 1206.4806
- ★ **MCFM: full analytic calculation for fast and numerically-stable evaluation.**

Stability

- ★ Matrix elements suffer from numerical instability as $p_T(Z) \rightarrow 0$ even though they are completely finite in that limit.
- ★ Important to ensure that implementation is stable there since a fairly substantial contribution to the total cross section comes from the low p_T region.

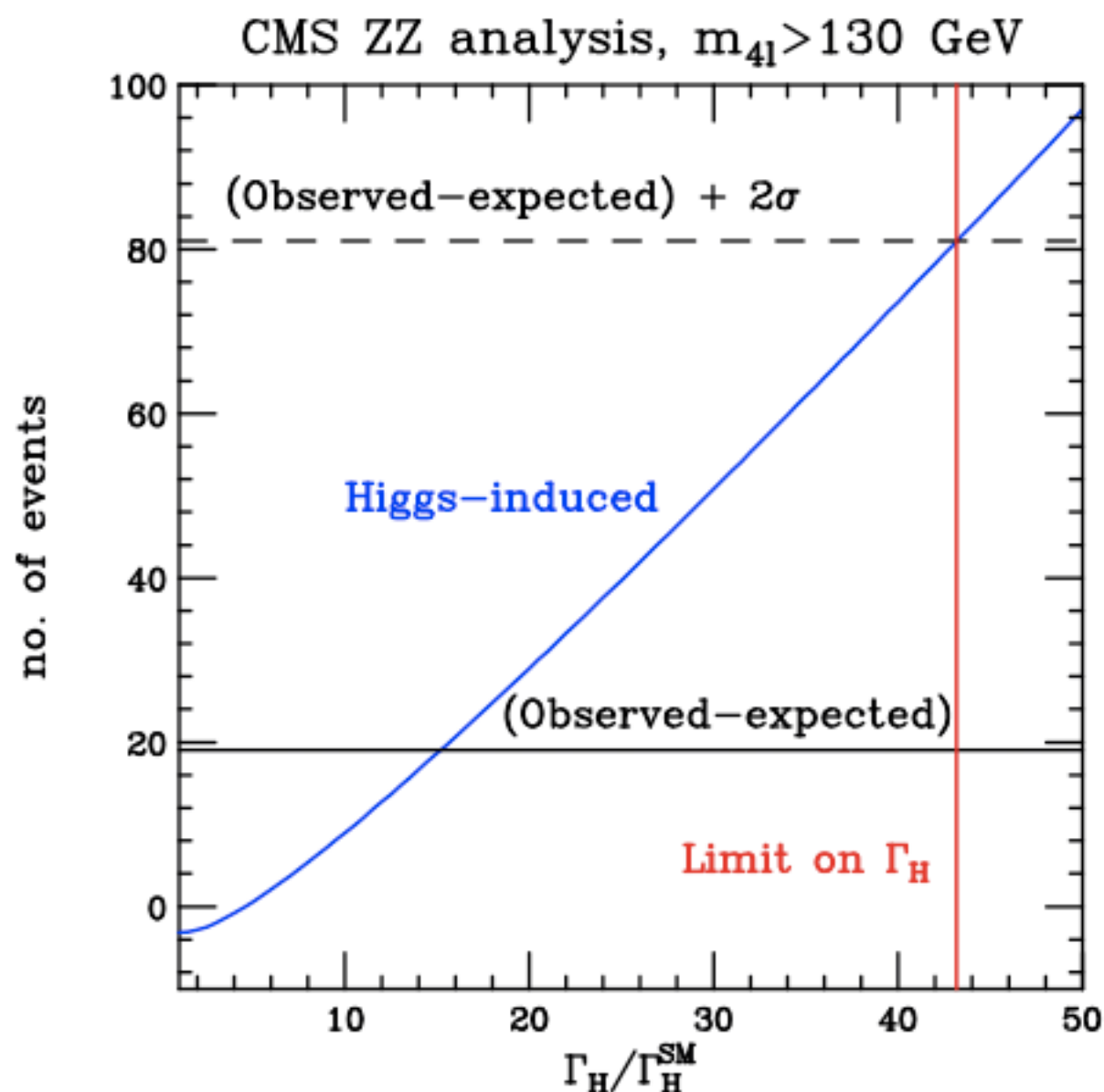


The big picture



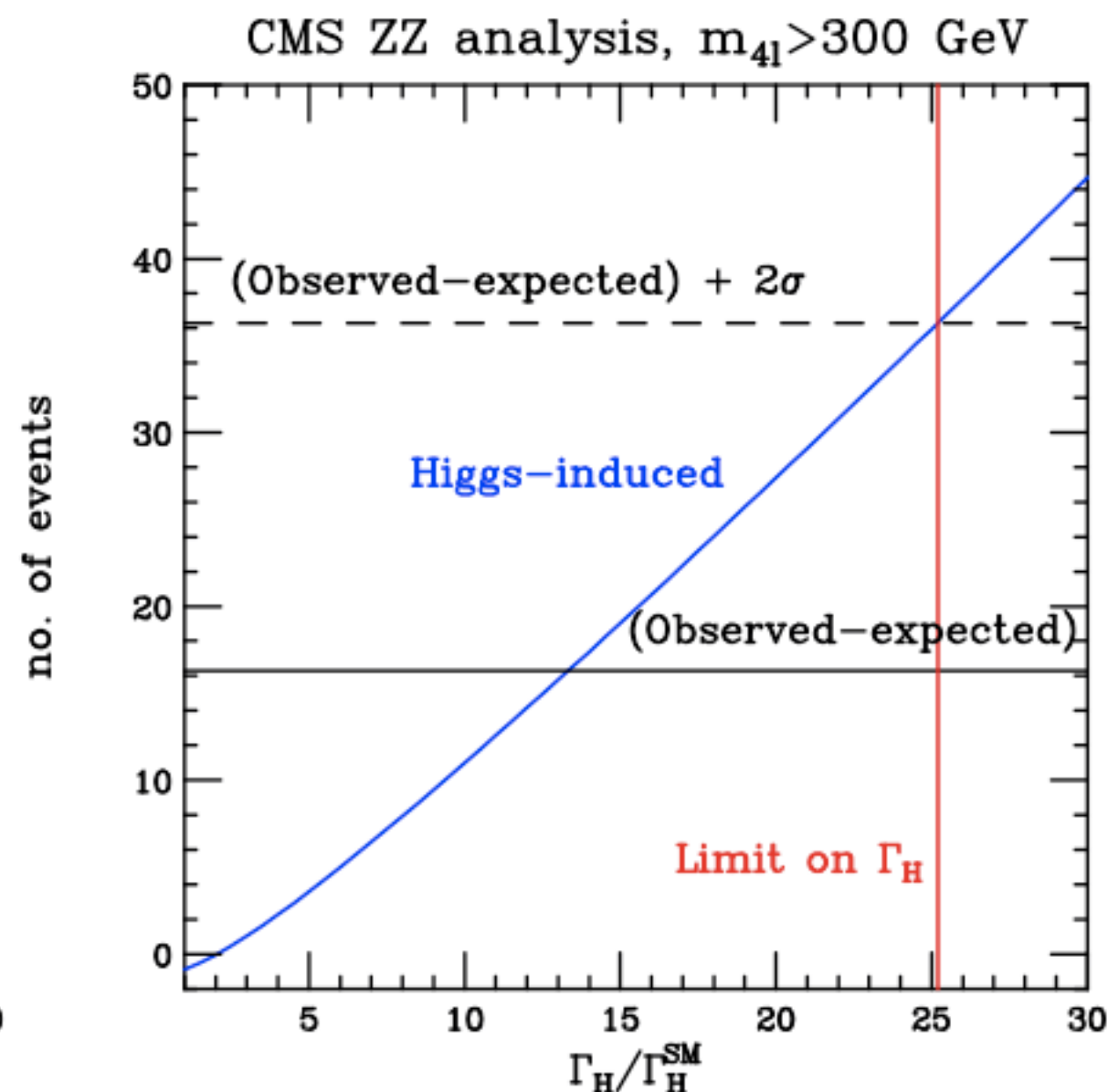
- ★ Continuum ($q\bar{q}$) background 1-2 orders of magnitude larger throughout most of range.
- ★ Destructive interference clear for $m_{4l} > 400$ GeV.
- ★ Cannot describe off-peak region without proper treatment of interference.
- ★ Difficult to observe effect (in the SM) since strong pdf suppression, so little rate.

Theorists' estimate



expected (no H): 432 ± 31

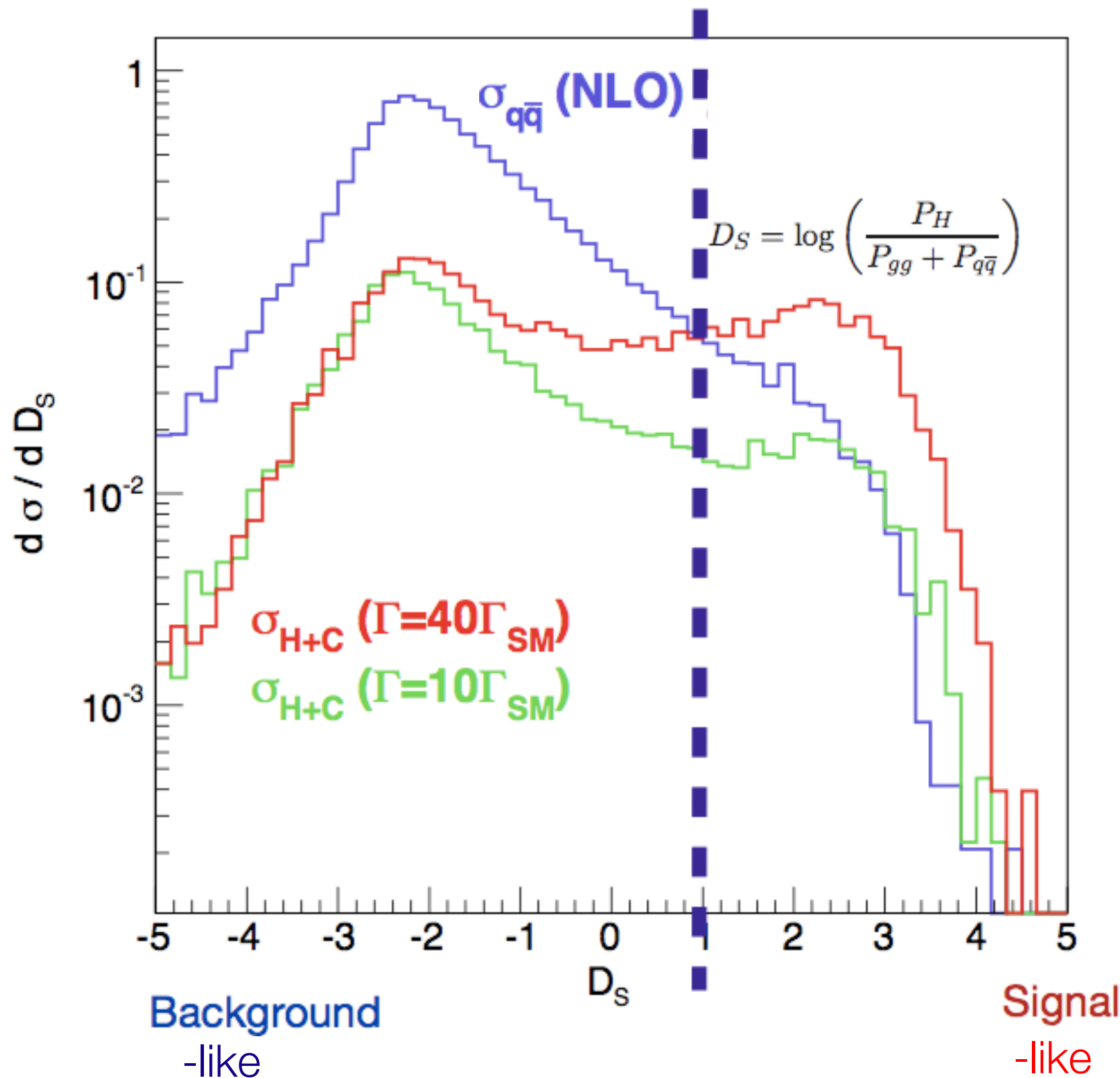
$$\Gamma_H < 43.2 \Gamma_H^{SM} \text{ at } 95\% \text{ c.l.}$$



expected (no H): $71 \pm (10?)$

$$\Gamma_H < 25.2 \Gamma_H^{SM} \text{ at } 95\% \text{ c.l.}$$

Matrix element method



★ Use MCFM to compute discriminant that isolates gluon-related contributions that are sensitive to width.

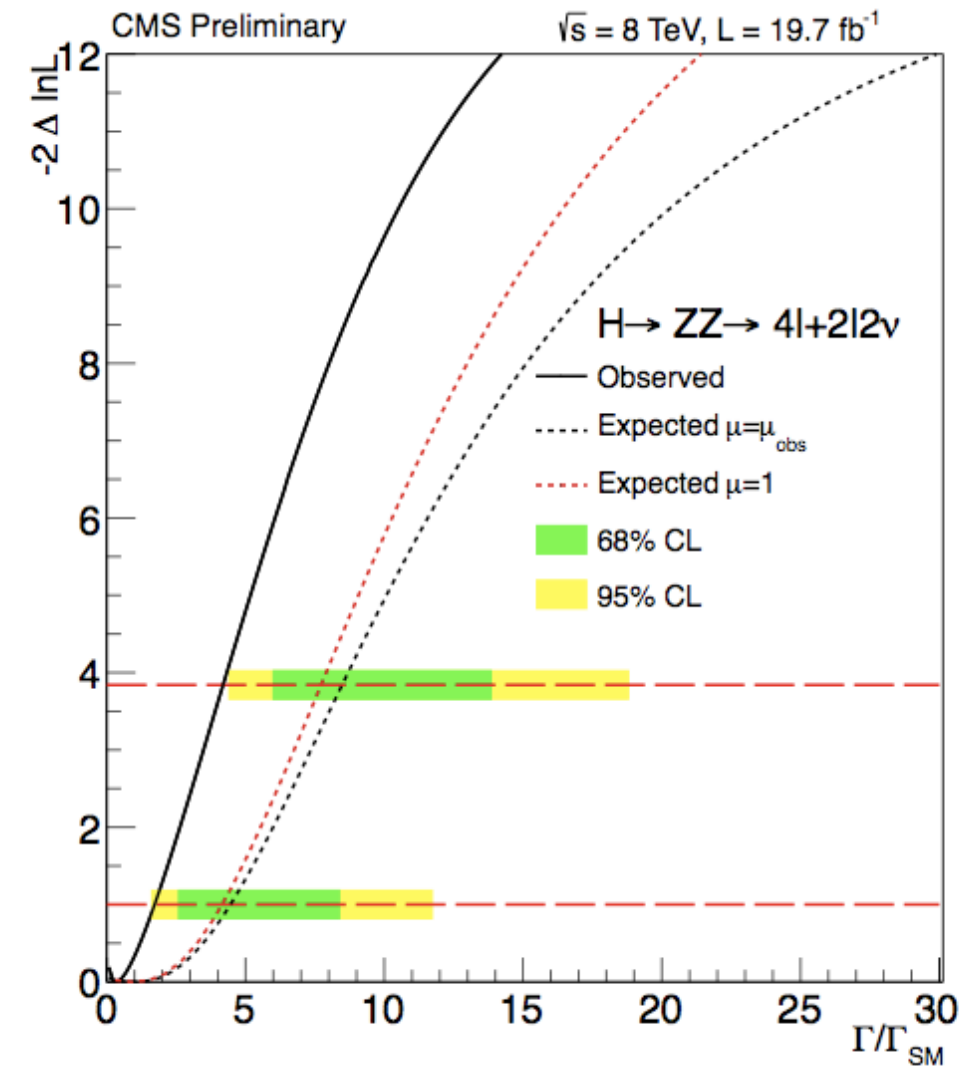
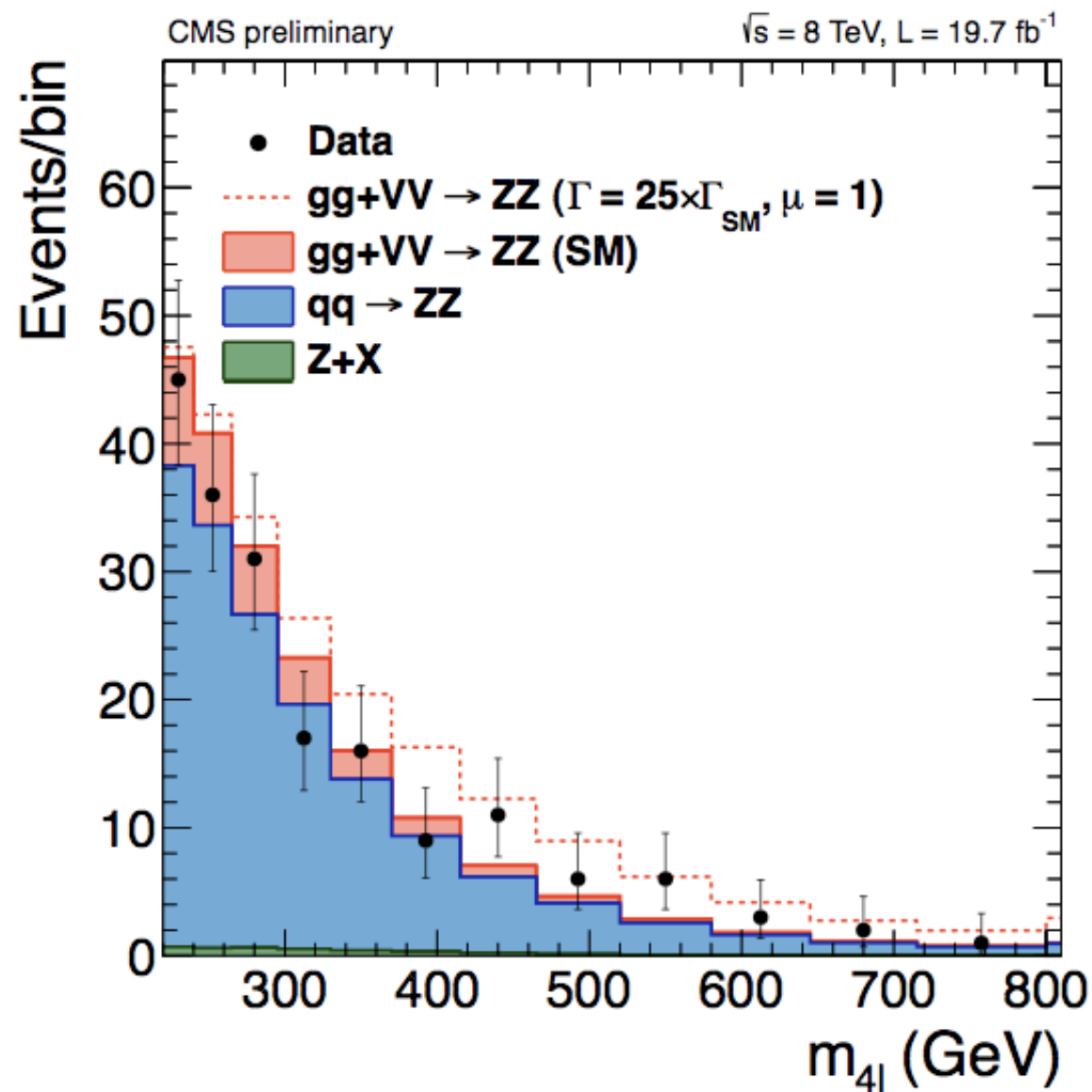
★ Using an analysis that roughly mimics the CMS results found before, bound can be improved:

$$\Gamma_H < (15.7^{+2.9}_{-3.9}) \Gamma_H^{SM} \text{ at 95\% c.l.}$$

★ This procedure adopted by ATLAS and CMS.

The CMS result

PAS HIG-14-002



$\Gamma_H < 4.2 \times \Gamma_H^{\text{SM}}$ at 95% confidence

The WW channel

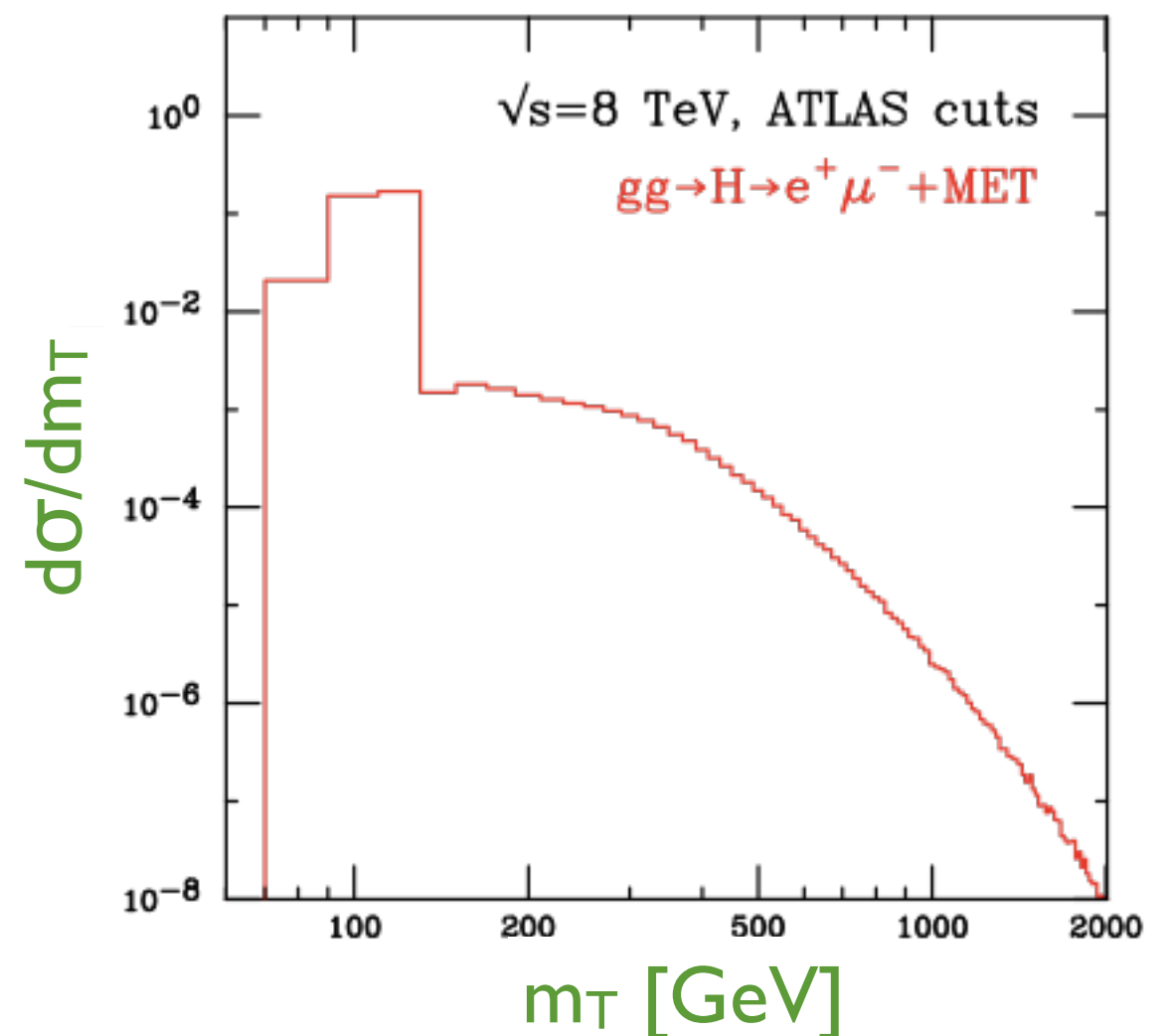
- ★ The ZZ channel is convenient: well-measured leptons allow the Higgs boson lineshape to be mapped out and peak/off-shell regions directly identified.
- ★ However, exact mapping of lineshape is not crucial, just need well-separated regions corresponding to on- and off-resonance.
- ★ Try to play the same game in WW channel:

$$gg \rightarrow W^+ W^- \rightarrow e^+ \mu^- \nu_e \bar{\nu}_\mu$$

- ★ As proxy for invariant mass, use transverse mass of WW system:

$$M_T^2 = (E_T^{miss} + E_T^{\ell\ell})^2 - |\mathbf{p}_T^{\ell\ell} + \mathbf{E}_T^{miss}|^2$$

- ★ Some features washed out, but clear separation between peak and tail remains.



WW vs ZZ

★ Advantages:

- ▶ threshold for two real W's much closer than for two real Z's
- ▶ branching ratio into leptons also larger
- ▶ combined, two orders of magnitude more events:

$$\text{Br}(H \rightarrow WW) \times \text{Br}(W \rightarrow \ell\nu)^2 = 2.7 \times 10^{-3}$$

$$\text{Br}(H \rightarrow ZZ) \times \text{Br}(Z \rightarrow \ell^+\ell^-)^2 = 3.2 \times 10^{-5}$$

★ Disadvantages:

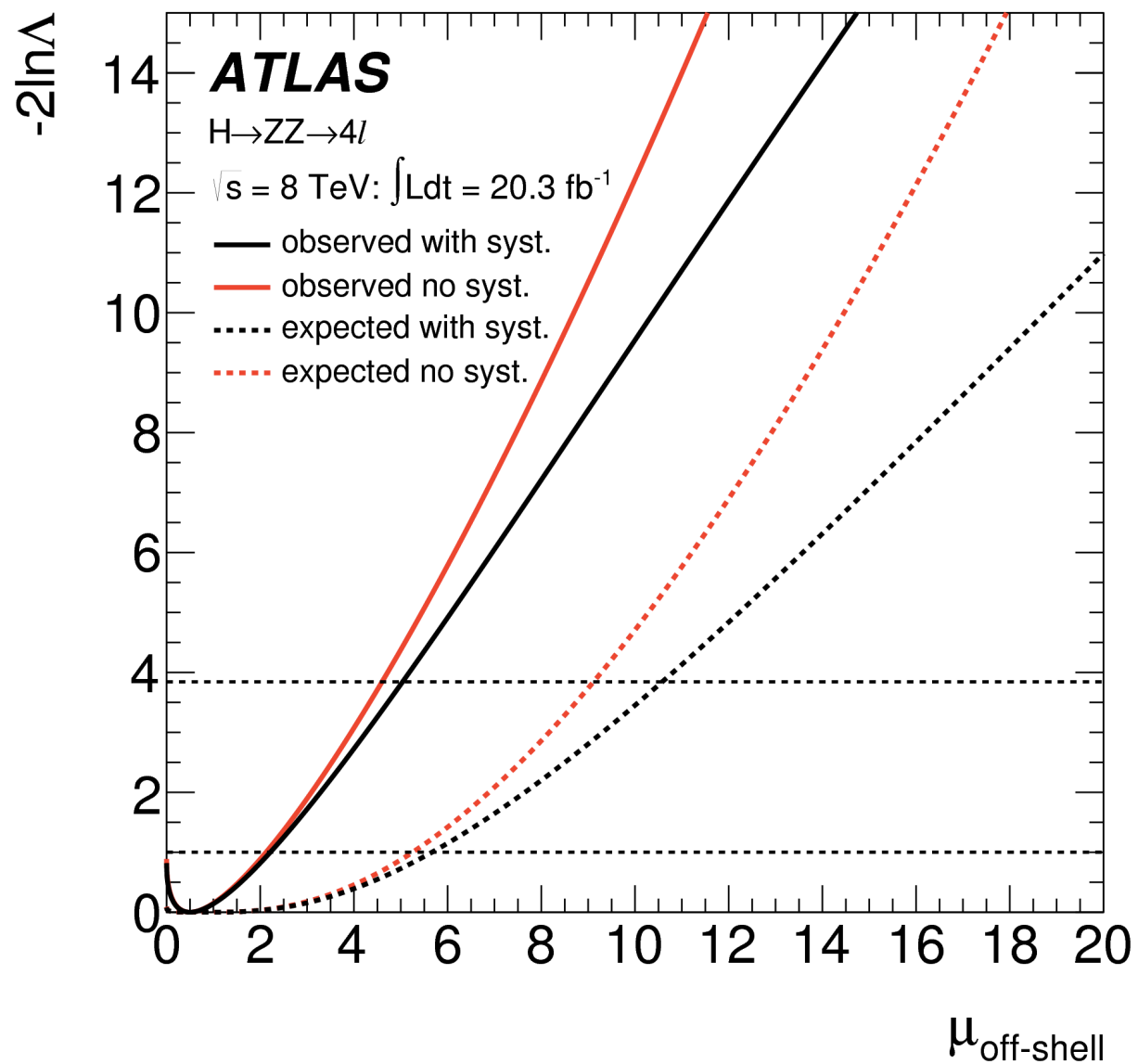
- ▶ much less clean so many more backgrounds, especially top-related ones that require a jet-veto to control
- ▶ even observing the on-shell Higgs boson in this channel is not easy.

Estimated sensitivity about a factor of three worse for WW than ZZ

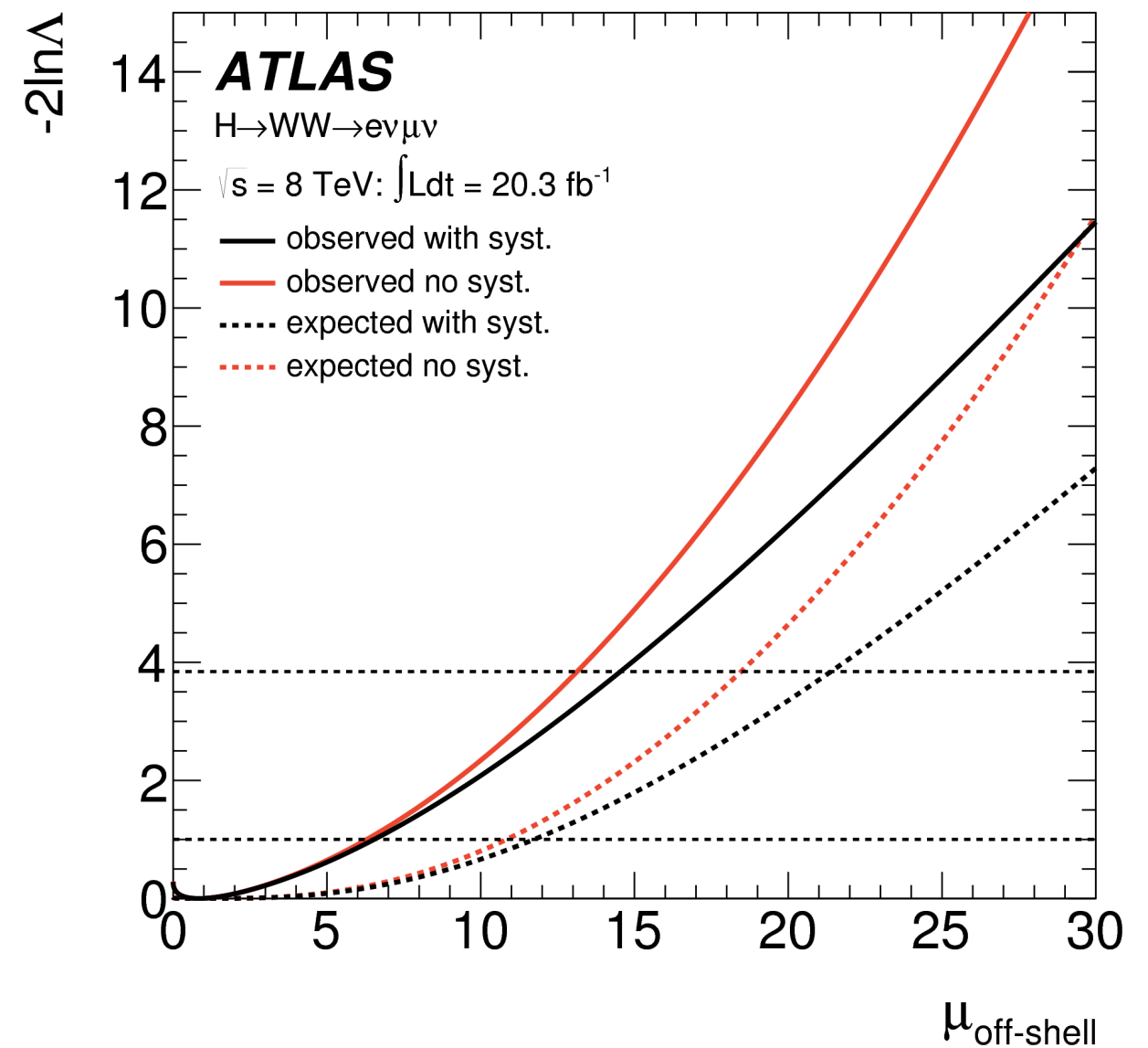
MCfM: 1312.1628

ATLAS comparison of ZZ, WW

arXiv: 1503.01060



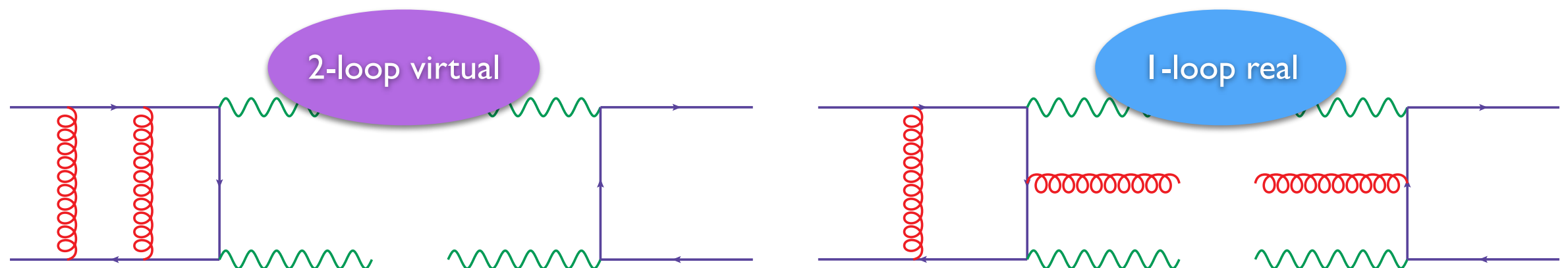
ZZ



WW

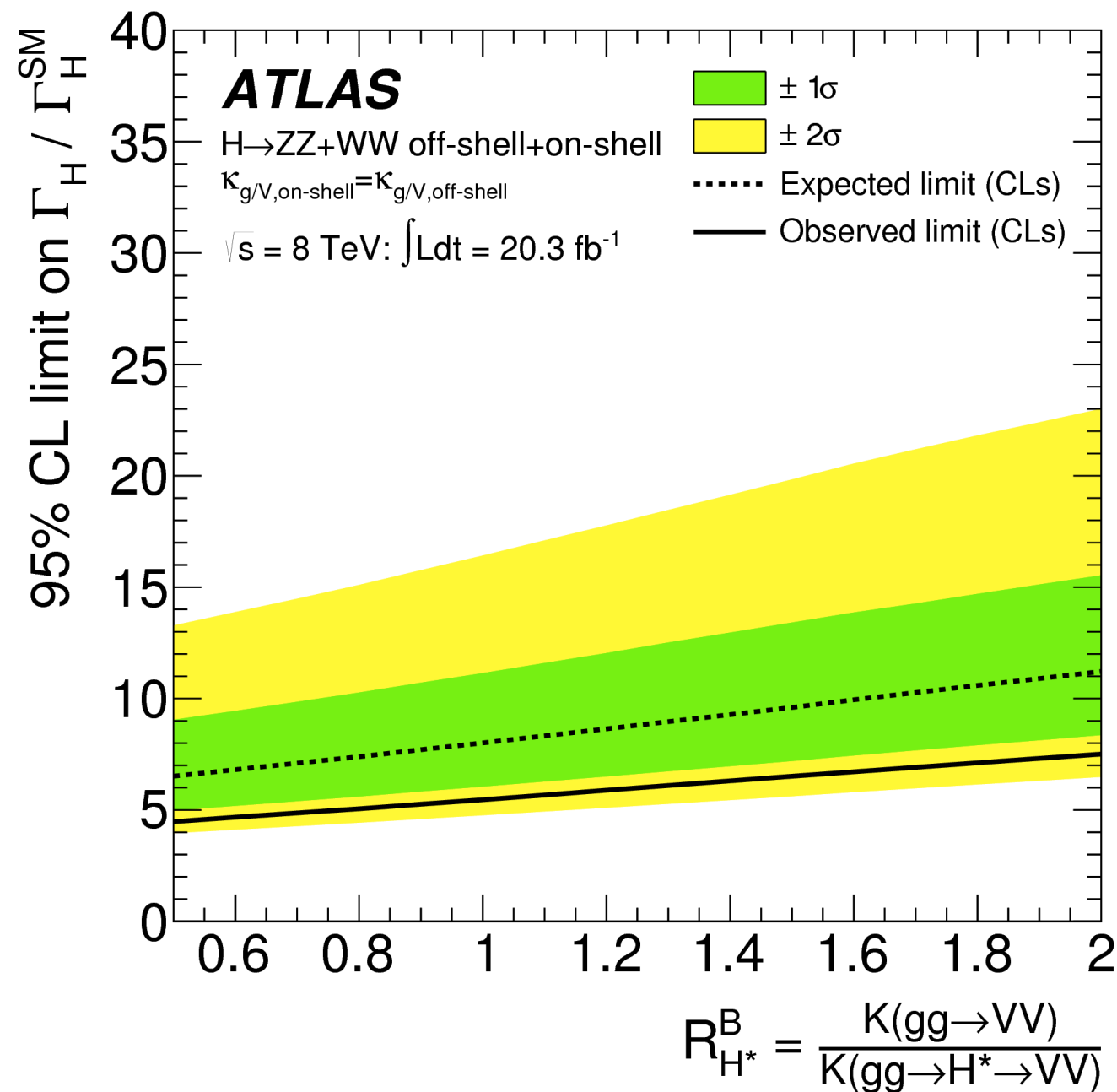
Caveat: higher orders

- ★ Despite the presence of a loop, the effect of the interference is computed at LO; however the Higgs contribution alone is known to (at least) NNLO.
- ★ Can assume the higher-order corrections to the interference scale in the same way, with some additional uncertainty (CMS strategy so far).
- ★ This is supported by soft gluon approximation of the NLO and NNLO result, which hints at a similar K-factor with perhaps a 30% uncertainty.
- ★ But we will only know for sure when the interference is calculated to NLO: i.e. 2-loop virtual and 1-loop real radiation contributions.



- ★ In the meantime, a good strategy is to consider full gg K-factor unknown.

ATLAS result vs. K-factor

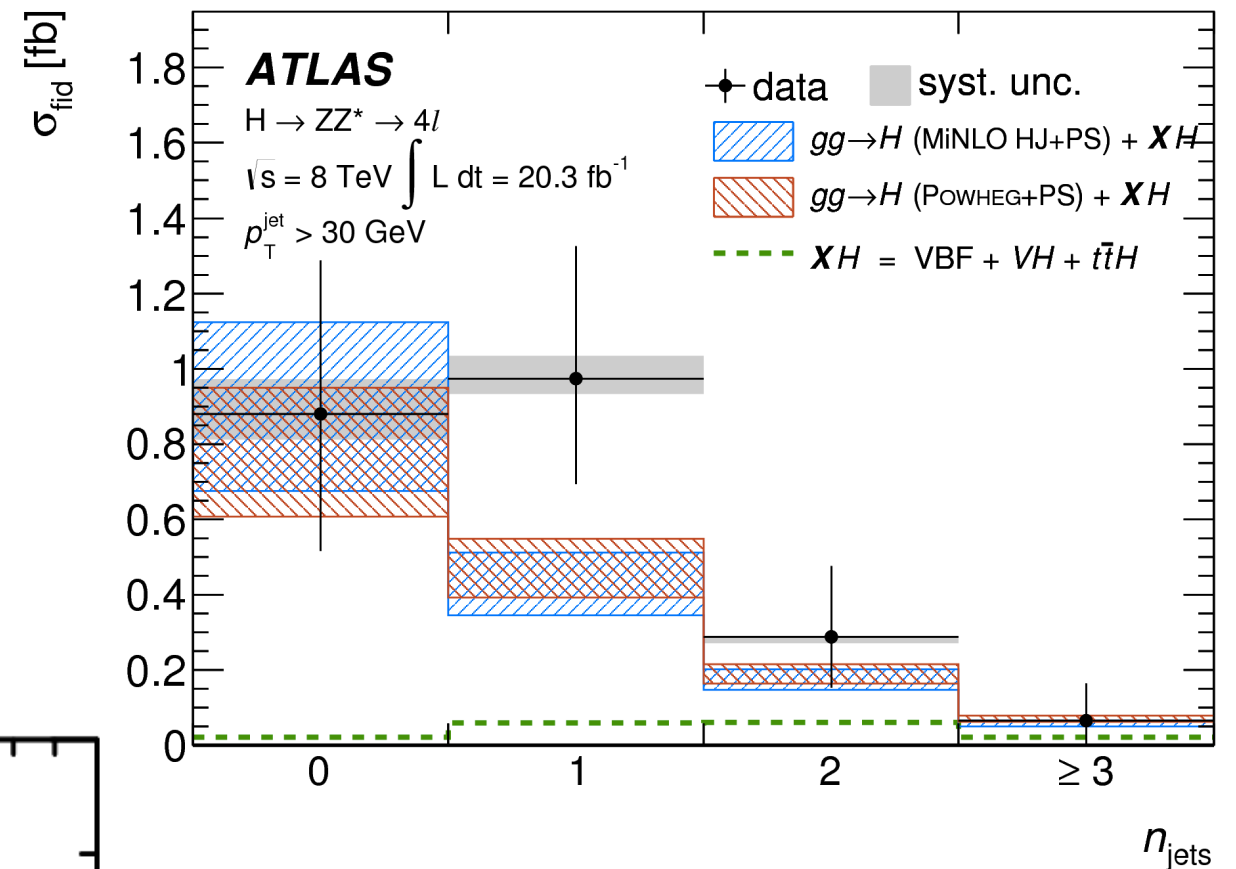
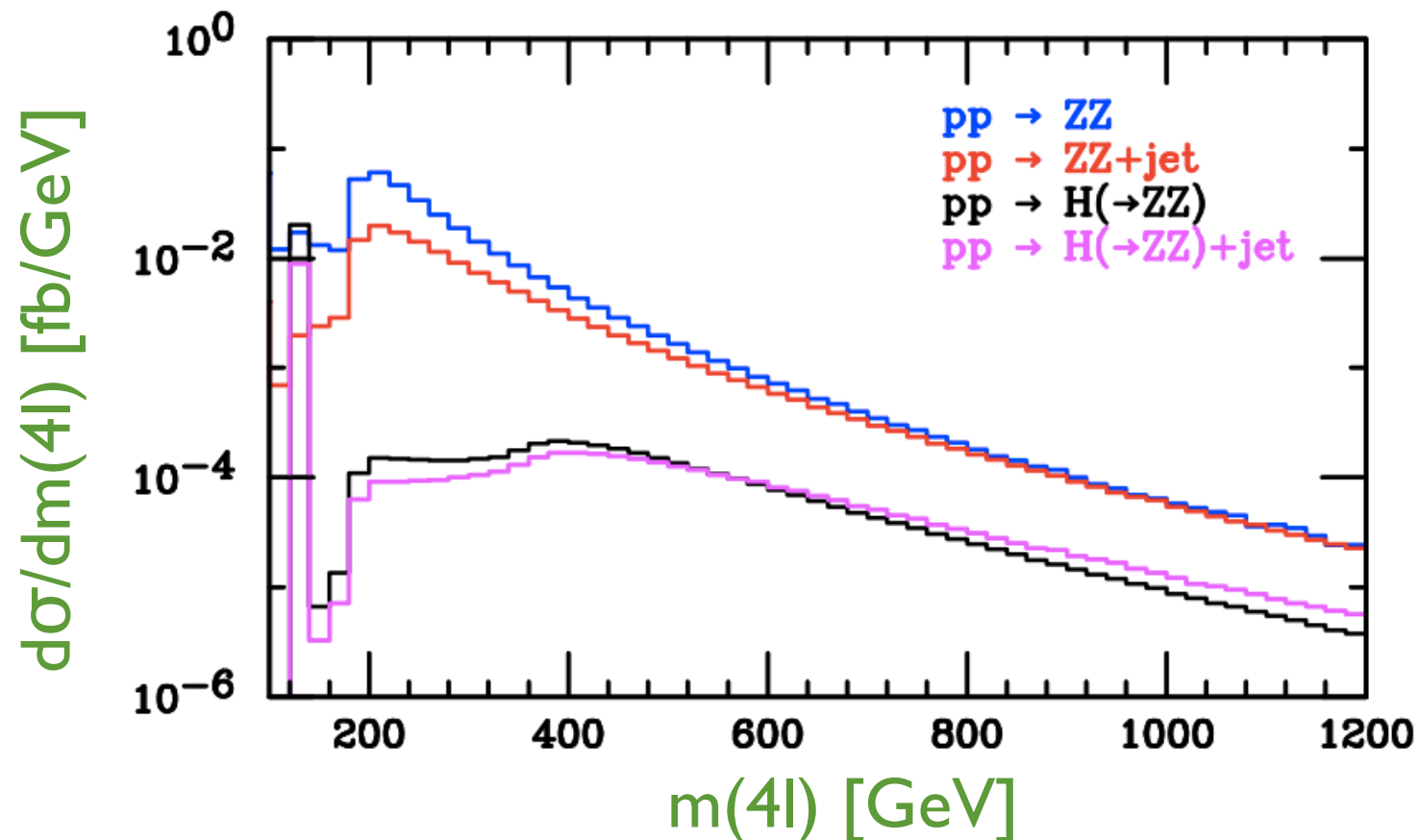


95% CL upper limit on $\Gamma_H / \Gamma_H^{\text{SM}}$ in the range 4.5–7.5

Extension to other channels

What about Higgs+jets?

- ★ Production by gluon fusion means that there are a **significant number of events where the Higgs boson is accompanied by hard jets.**
- ★ Can the jet-binned cross-sections provide additional information?

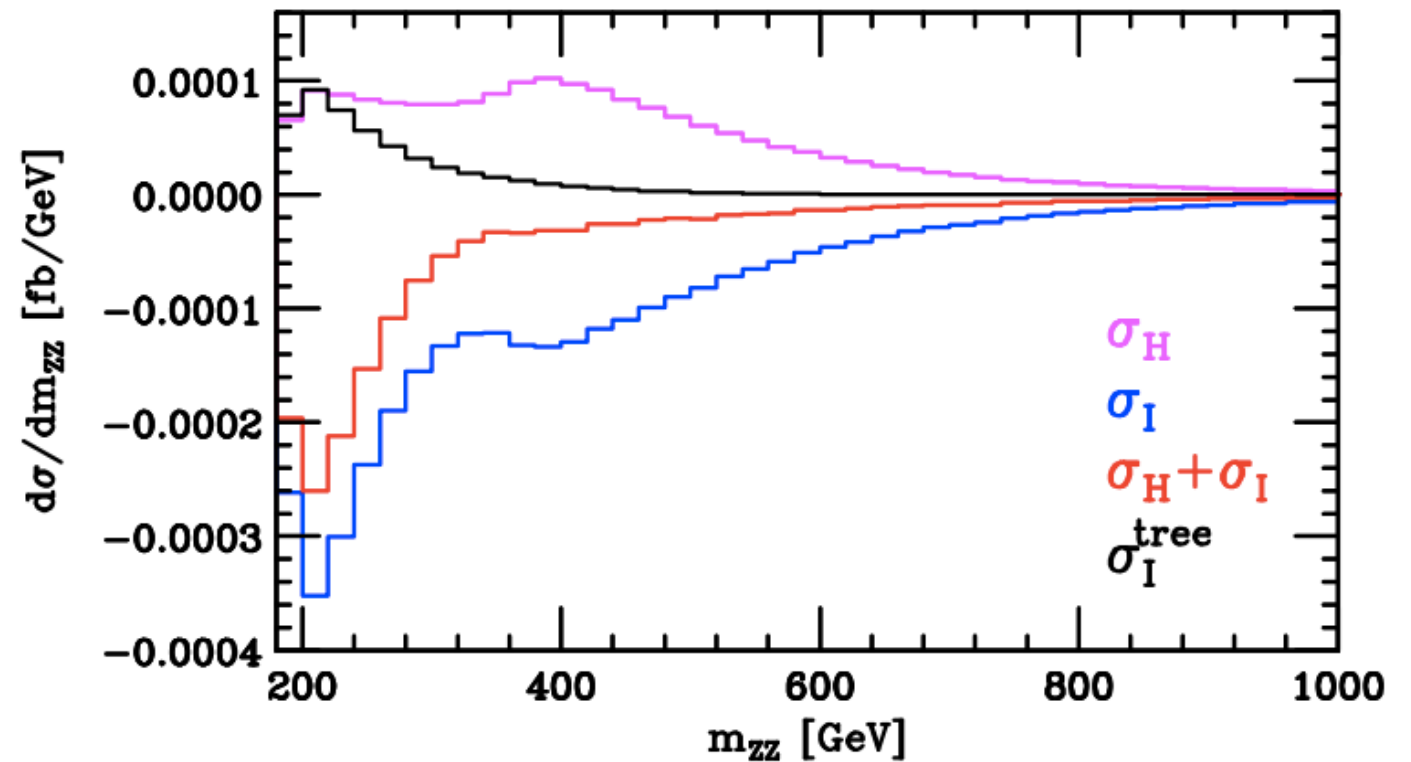


- ★ For one jet, unequivocal yes!
- ★ Off-shell tail is about the same size, while leading SM background is smaller.

MC_{FM}: 1409.1897

ZZ+jet results

- ★ Calculation very challenging even at one-loop; simplified by use of on-shell Z bosons (well-justified in off-shell region).
- ★ One of the ingredients needed to extend inclusive analysis to NLO.
- ★ At this order in the couplings, additional contributions arise from interference with tree-level background amplitudes.
- ★ Expect similar sensitivity to inclusive case.



ZZ+jet: $\sigma_{off,ZZ+jet}^{H+I}(m_{ZZ} > 300 \text{ GeV}) = 0.0280 \left(\frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 0.0392 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}} \text{ fb}$

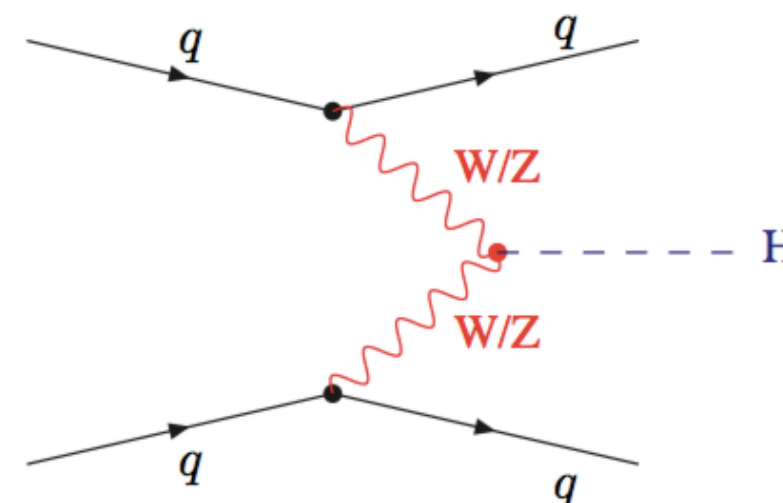
ZZ inclusive: $\sigma_{off,ZZ}^{H+I}(m_{ZZ} > 300 \text{ GeV}) = 0.0323 \left(\frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 0.0468 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}} \text{ fb}$

Caveat: model dependence

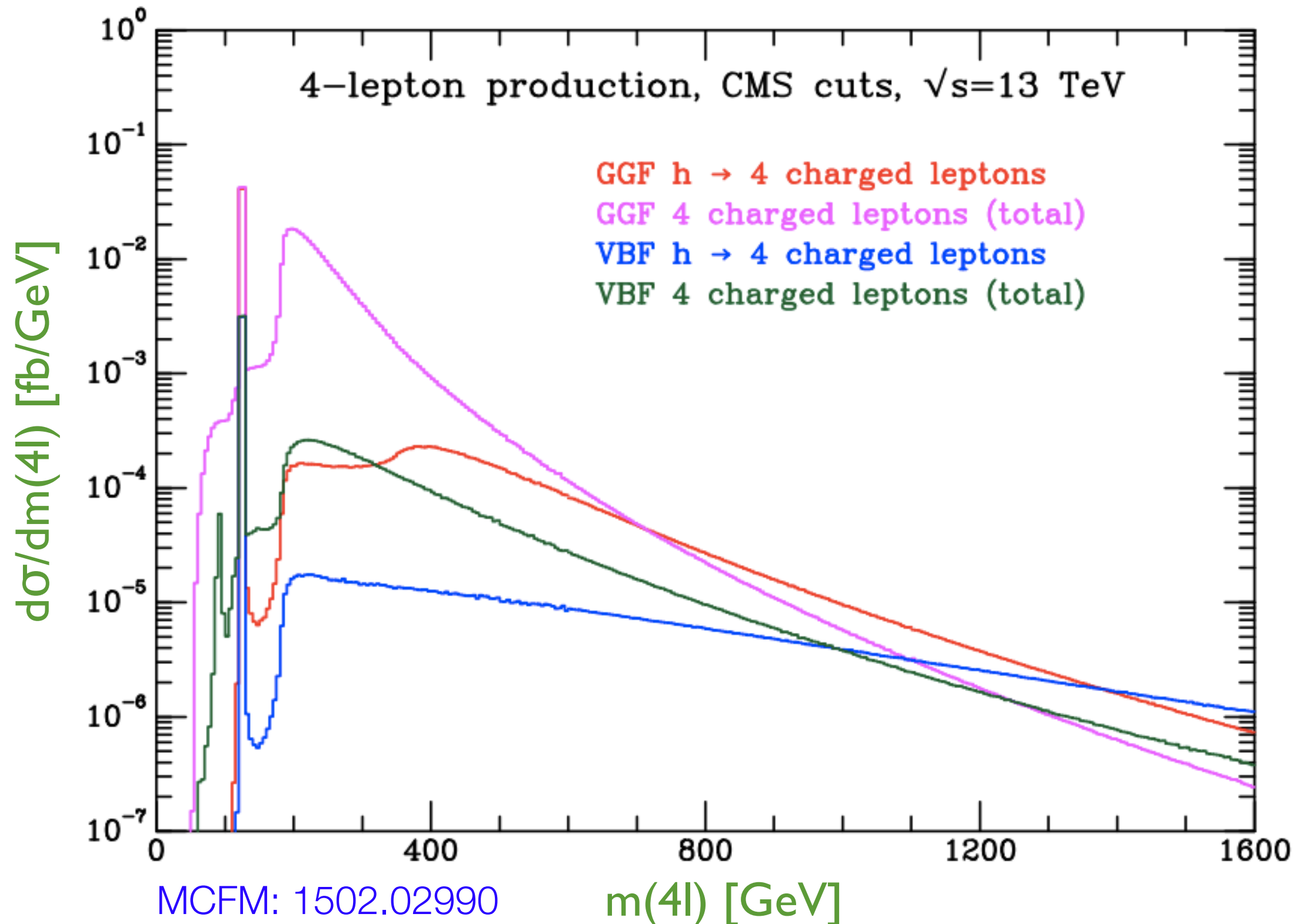
- ★ The bounds on the width presented here assume that on- and off-shell couplings of the Higgs boson are the same.
- ★ This is an assumption that can be easily violated in extensions of the Standard Model that may, or may not, alter the width.
 - ▶ new heavy particles running around the loops provide a natural energy-dependence of the coupling, as new internal thresholds are crossed.
[Englert, Spannowsky: 1405.0285](#)
- ★ The interpretation of these measurements in terms of a width constraint is therefore model-dependent.
- ★ Two interpretations:
 - ▶ **constraint on the width in certain classes of model**, including an important consistency check of the Standard Model;
 - ▶ **constraint on the off-shell coupling.**

VBF channels

- ★ Much of the model-dependence results from possible contamination of the off-shell coupling through unknown new particles in the loops.
- ★ This can be alleviated by moving to tree-level processes: vector boson fusion.
- ★ Of course, existing analyses receive some contribution from VBF processes already, although at a sub-dominant level.
- ★ **VBF cross section approximately 8% of gluon fusion**, will become amenable to dedicated studies in a similar vein in upcoming runs.
- ★ Importance of high-mass region well-appreciated for a long time due to the importance of longitudinal modes that are a consequence of EWSB.
 - ▶ similar pattern of destructive interference.

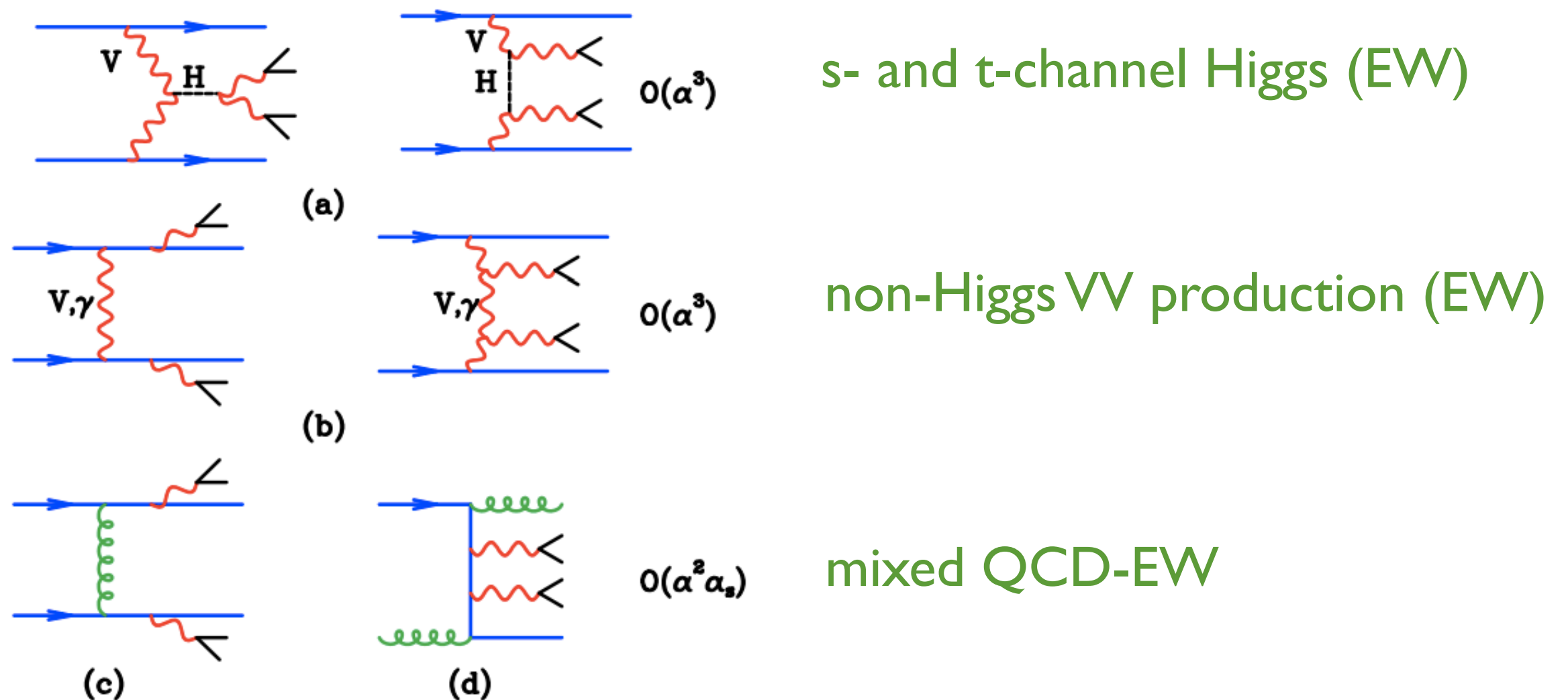


Comparison of GGF and VBF



VBF and VBS

- ★ To properly treat the VBF channels, with decay of the Higgs boson into a vector boson pair VV , it is essential to include all diagrams leading to the $VV+2\text{jet}$ state.
- ★ Here “VBF” is a loose designation, including both vector boson scattering (“VBS”) contributions and all other diagrams at the same order in the couplings.



Size of rates

- ★ Off-shell 13 TeV cross-sections computed at LO using MCFM, in VBF-like region.
 - ▶ rapidity gap between jets, opposite hemispheres, large dijet invariant mass.
 - ▶ basic cuts on leptons and rudimentary cut to reduce top backgrounds.

Process	Events in 100 fb ⁻¹	
	EW process	mixed QCD-EW
W	87	96
W	27	2
W	9	0
W	20	37
W	10	18
ZZ(4l)	4	3

Coupling framework

- ★ As before, use interim framework where **H couplings to W,Z scale in same way:**

$$\frac{\Gamma_{WW}}{\Gamma_{WW}^{SM}} = \kappa_V^2, \quad \frac{\Gamma_{ZZ}}{\Gamma_{ZZ}^{SM}} = \kappa_V^2$$

- ★ $\kappa_V < 1$ better motivated theoretically, $\kappa_V > 1$ corresponds to C.-M. width constraint.
- ★ Can be related to dimension-six operator in effective field theory:

$$\mathcal{L}_{HD} = F_{HD} \operatorname{tr} \left[\mathbf{H}^\dagger \mathbf{H} - \frac{v^2}{4} \right] \cdot \operatorname{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right]$$

$$\kappa_V = 1 + F_{HD} \frac{v^2}{2}$$

- ★ $\kappa_V = 0$ (no Higgs boson) corresponds to $F_{HD} \approx 30 \text{ TeV}^{-2}$ which is outside the validity of the EFT; conversely, TeV scales correspond to a few percent deviations of κ_V .

Existing bounds

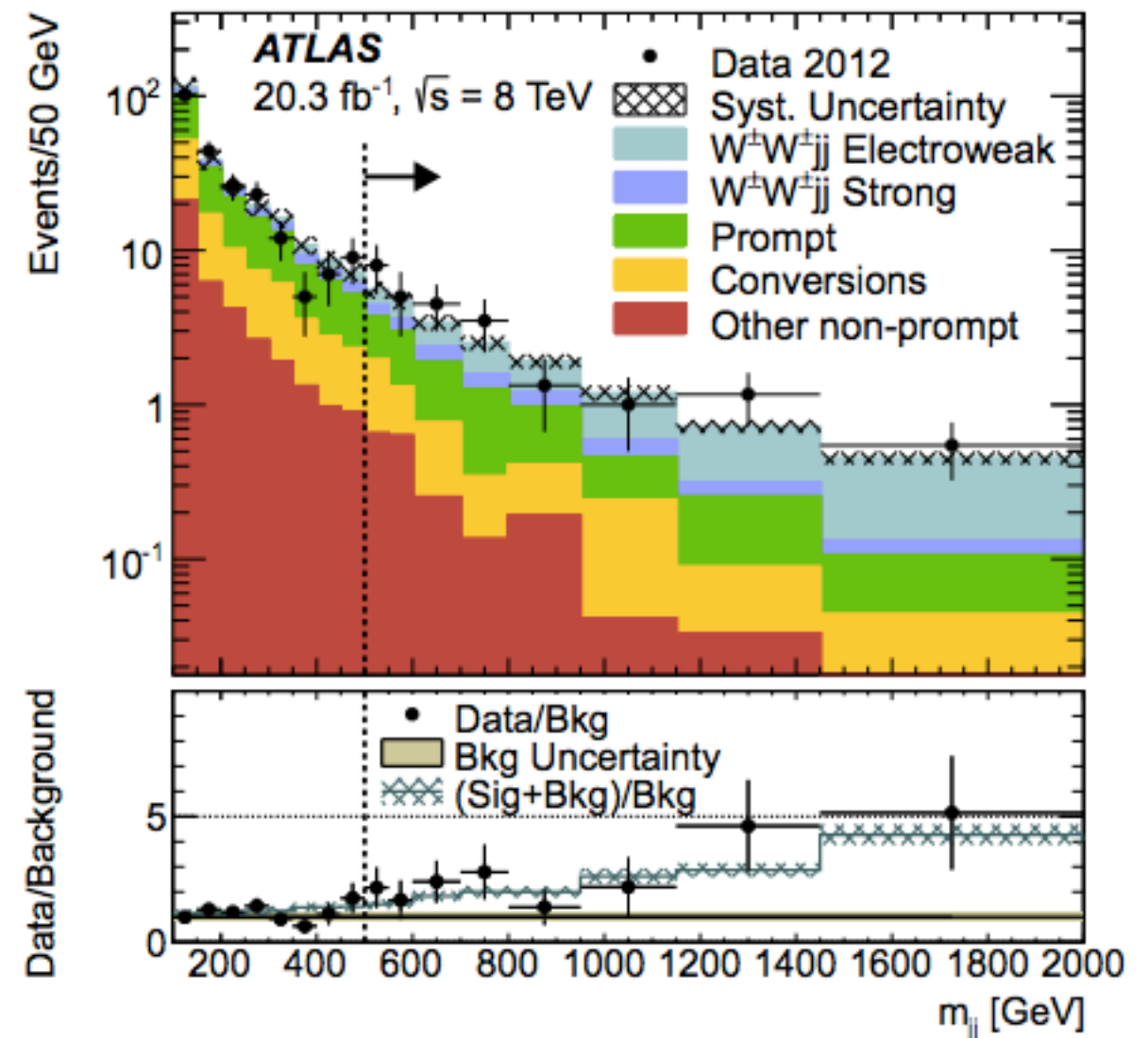
- ★ ATLAS has already provided evidence for same-sign W production in association with two jets.

[arXiv:1405.6241](https://arxiv.org/abs/1405.6241)

- ★ The expected number of events is small, so only relatively mild VBF cuts can be applied.
- ★ Nevertheless, the result can still be interpreted as a weak bound on the coupling strengths.

$$\kappa_V < 7.8$$

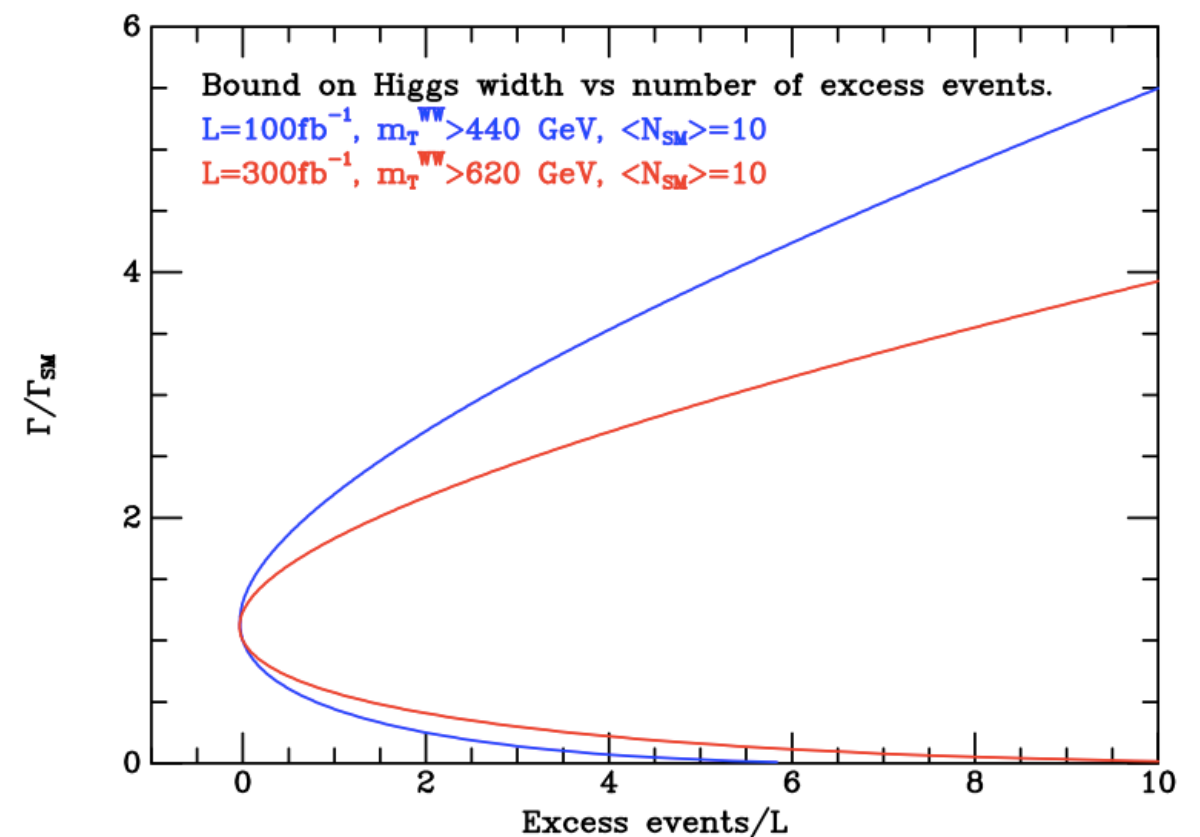
$$\Gamma_H < 60.8 \times \Gamma_H^{SM}$$



Reasonable bounds for a statistics-limited analysis in a channel without s-channel Higgs resonance!

LHC runs 2 and 3

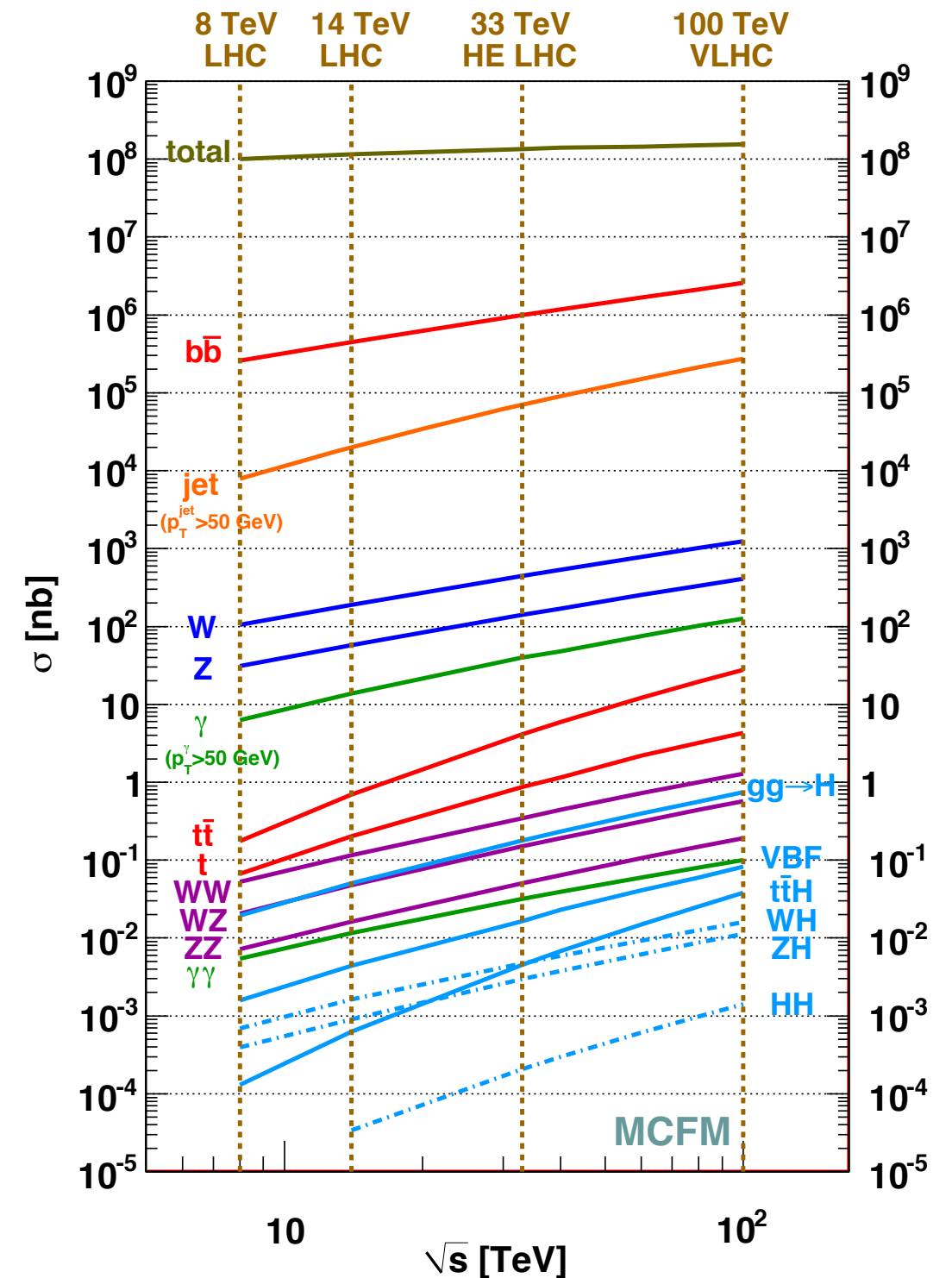
- ★ Simple analysis based on **Run 2 (100fb^{-1})** and **Run 3 (300fb^{-1})** at 13 TeV.
 - ▶ optimize cut that determines off-shell region.
 - ▶ trade-off as cut increases between better sensitivity and dwindling statistics.
- ★ In Run 2, only the same-sign WW process yields a lower bound on κ .
- ★ In Run 3, the opposite-sign W^-W^+ process may have sensitivity too (modulo handling backgrounds).
- ★ The same-sign processes always provide the most stringent limits, due to the lack of pollution from the mixed QCD-electroweak background.
- ★ **Sensitivity similar to GGF in Run 1.**



MCFM development

MCFM: recent additions

- ★ $gg \rightarrow VV$ processes, including vector boson decays, Higgs contributions, effect of identical-particle and WW/ZZ interference.
- ★ Triphoton, diphoton+jet, four-photon production, $Z\gamma\gamma$ and $Z\gamma$ +jet with photon fragmentation.
- ★ Single-top production with Higgs or Z boson (tH and tZ).
- ★ Production and decay of a top pair and a W boson ($t\bar{t}W$).
- ★ Dark matter production with mono-jet or mono-photon signatures.



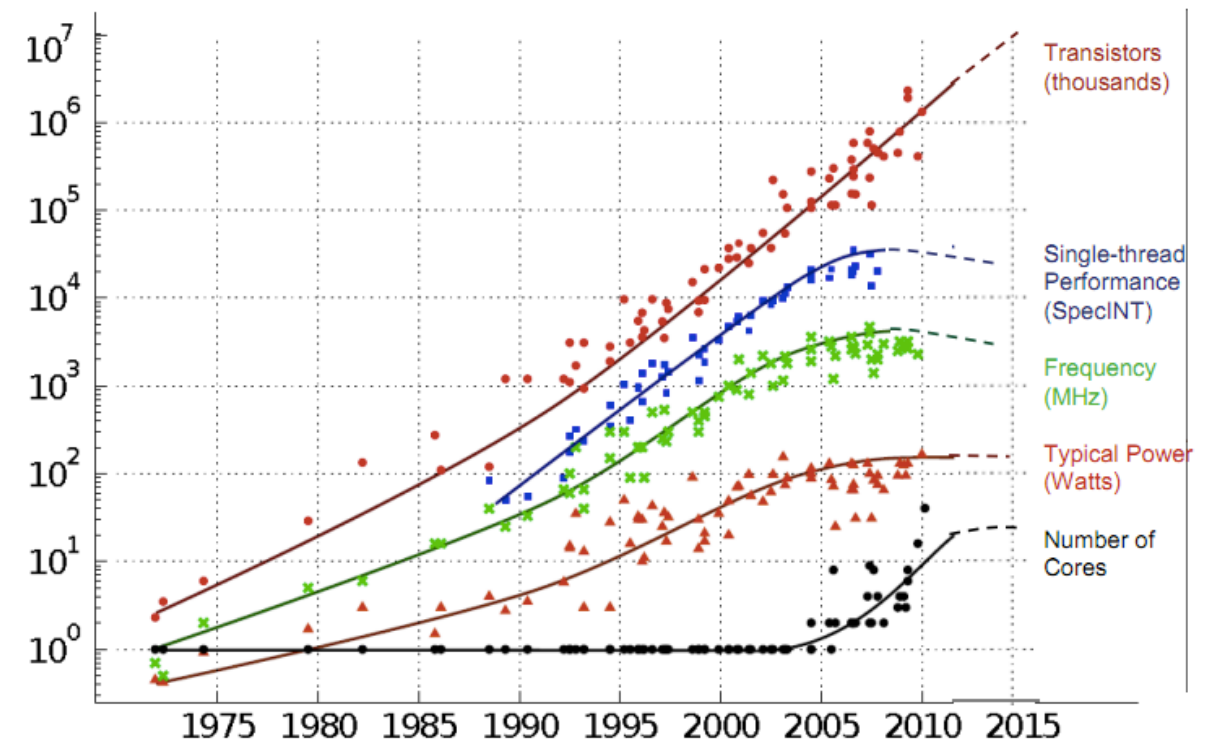
MCFM v7

- ★ Additions to the code that are coming soon:
 - ▶ **multi-threaded version** using OpenMP that will allow very fast generation of NLO predictions on multi-core processors.
 - ▶ evaluation of tree-level matrix elements using **Berends-Giele recursion** for both speed and access to high-multiplicity final states.
 - ▶ **inclusion of electroweak corrections** for select processes; will be completed in conjunction with Doreen Wackeroth and Jia Zhou (Buffalo).

MCFM-OMP

- ★ Continued growth in computing power (Moore's law) can only be realized by use of many parallel cores/threads.
 - ▶ imperative that HEP software can take advantage of this.
- ★ We chose the **OpenMP standard** to implement parallelism in MCFM
 - ▶ parallel structure is implemented using minor alterations to the code via compiler directives (comments).
- ★ Generation of many phase-space points in parallel but controlled by the same VEGAS integration parameters to obtain faster convergence.
 - ▶ care taken to ensure final **result independent of number of threads** used.

35 YEARS OF MICROPROCESSOR TREND DATA



Original data collected and plotted by M. Horowitz, F. Labonte, O. Shacham, K. Olukotun, L. Hammond and C. Batten
Dotted line extrapolations by C. Moore

Speed-up example

PP-> H(->bb)+ 2 jets @ NLO

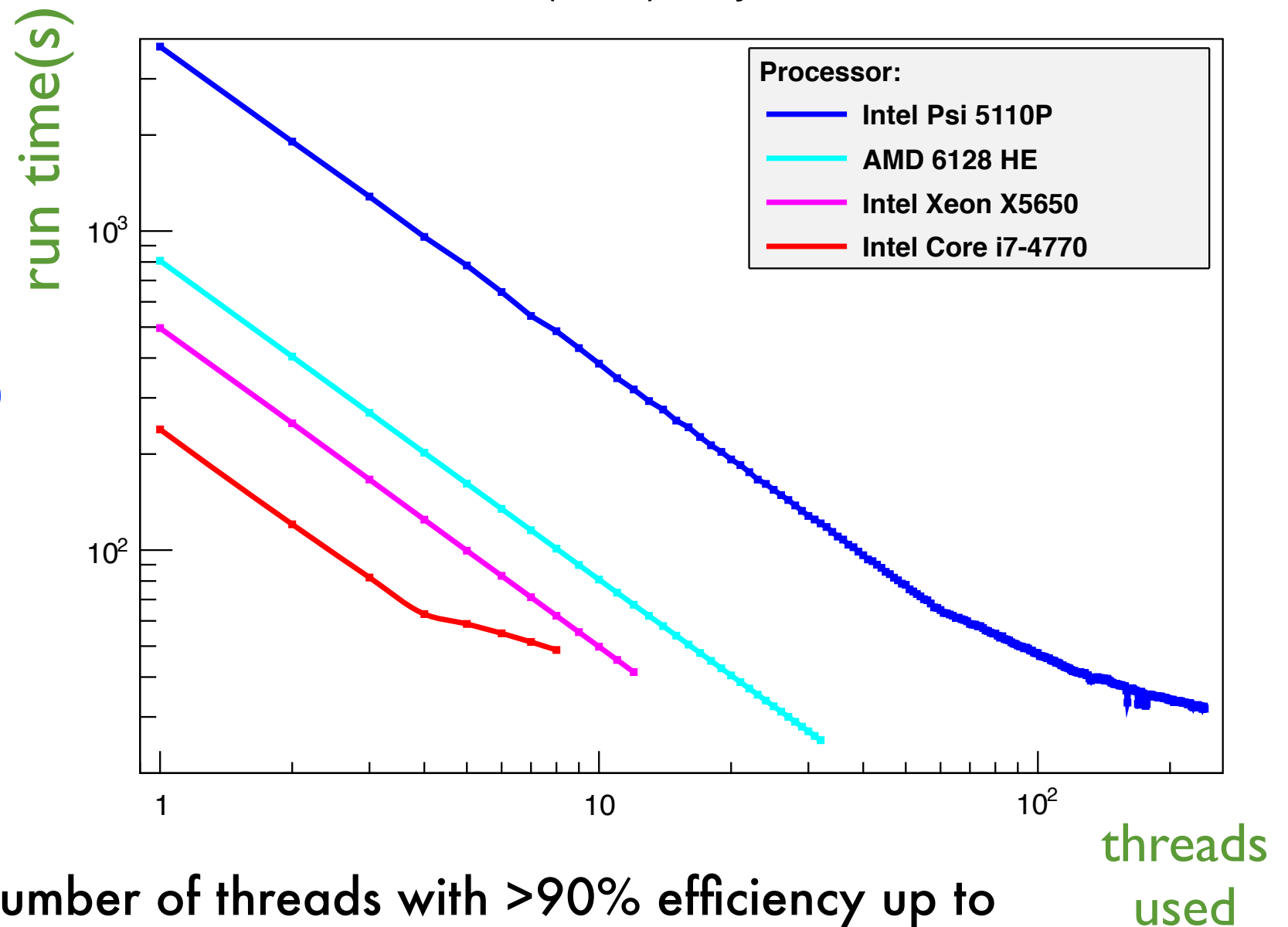
H+2 jets @ NLO: one of the most CPU-intensive calculations in MCFM

Intel Xeon-Phi (240 threads)

AMD Opteron (32 threads)

Intel Xeon (12 threads)

Intel i7 desktop (8 threads)



- ★ Acceleration scales with number of threads with >90% efficiency up to hardware limitations, e.g. for i7 > 4 threads, Xeon-Phi > 60 threads.
- ★ Single Xeon-Phi processor poor now (14x slower than single i7), but will improve.

Summary

★ Width and off-shell coupling bounds:

- ▶ powerful technique that is complementary to on-shell analyses.
- ▶ useful constraints from a number of decay modes and production channels: gluon fusion, in association with jets, VBF and VBS.
- ▶ performing multiple analyses will provide more robust bounds and help to mitigate model assumptions and uncertainties.
- ▶ more theoretical work remains to be done, e.g. higher-order corrections.

★ MCFM:

- ▶ provides a tool for performing many of the studies discussed above.
- ▶ development continues, with v7.0 to be released in the next couple of weeks.
- ▶ speed gain from use of multi-cores allows more complex calculations in future.

Backup slides

Other methods for the width

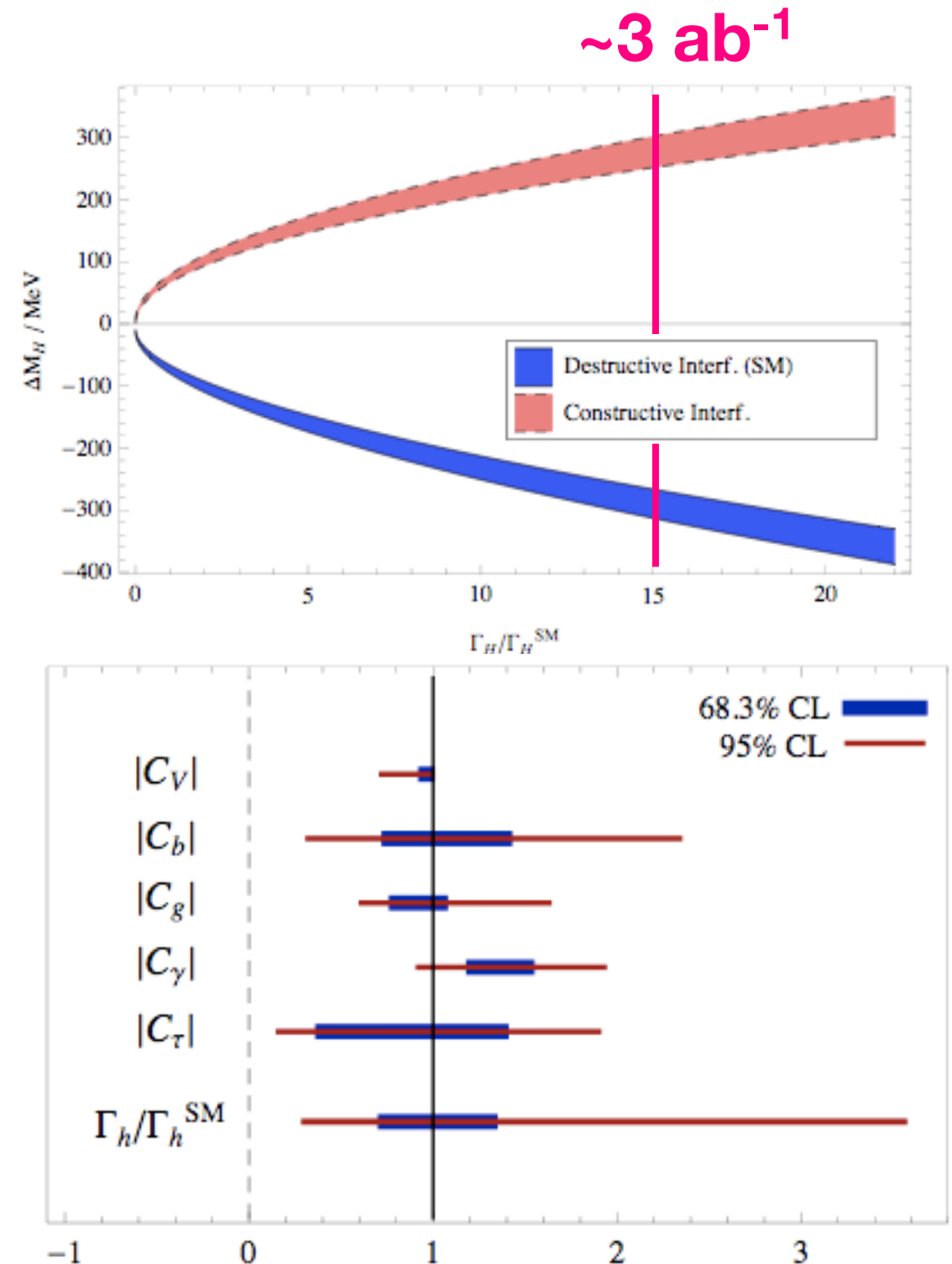
- ★ **Direct:** interferometry in diphoton decay; interference induces change in diphoton mass distribution that depends on the width.

Dixon, Li; 1305.3854

- ★ Require precise measurement of mass shift between ZZ and diphoton channels.

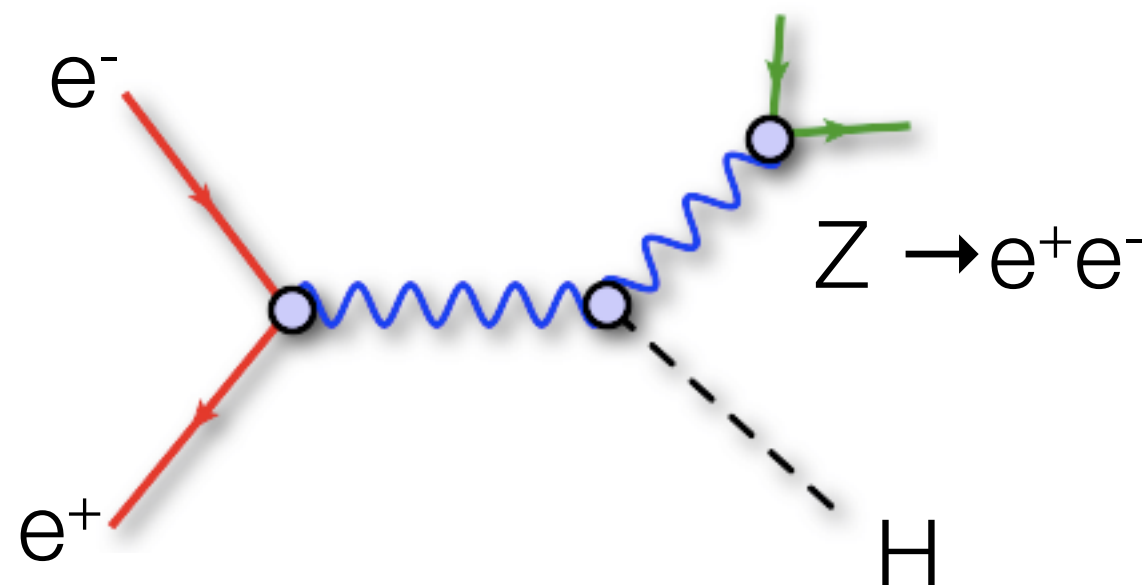
- ★ **Indirect:** global coupling fits; assume either that the coupling to W,Z takes the SM value, or is bounded by reasonable theoretical assumptions.

Dobrescu, Lykken; 1210.3342



Future linear collider

- ★ The width of the Higgs boson is a key deliverable of future lepton colliders.
- ★ Clear strategy for a LC.



- Tag ZH events where recoil mass is consistent with a Higgs boson
→ measurement of $\sigma(ZH)$
- Measurement of $H \rightarrow ZZ$ rate then determines $\text{Br}(H \rightarrow ZZ)$

$$\Gamma_H = \Gamma(H \rightarrow ZZ) / \text{Br}(H \rightarrow ZZ)$$

$$\propto \sigma(ZH) / \text{Br}(H \rightarrow ZZ)$$

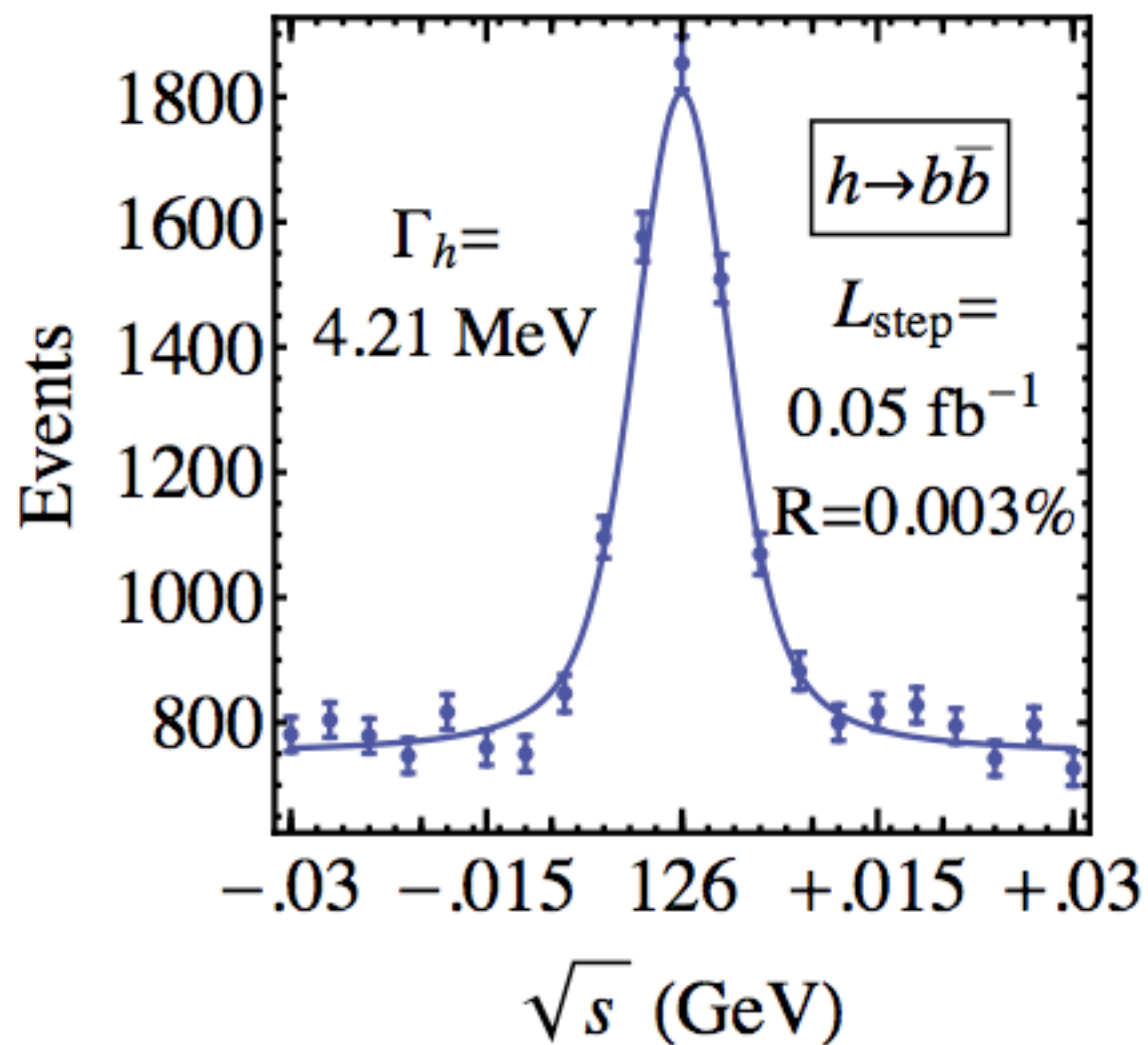
- ★ At 350 GeV and beyond (CLIC/TLEP), similar analysis through WW fusion.

Facility	ILC			ILC(LumiUp)	TLEP (4 IP)		CLIC		
\sqrt{s} (GeV)	250	500	1000	250/500/1000	240	350	350	1400	3000
$\int \mathcal{L} dt$ (fb^{-1})	250	+500	+1000	1150+1600+2500 [†]	10000	+2600	500	+1500	+2000
$P(e^-, e^+)$	(-0.8, +0.3)	(-0.8, +0.3)	(-0.8, +0.2)	(same)	(0, 0)	(0, 0)	(0, 0)	(-0.8, 0)	(-0.8, 0)
Γ_H	12%	5.0%	4.6%	2.5%	1.9%	1.0%	9.2%	8.5%	8.4%

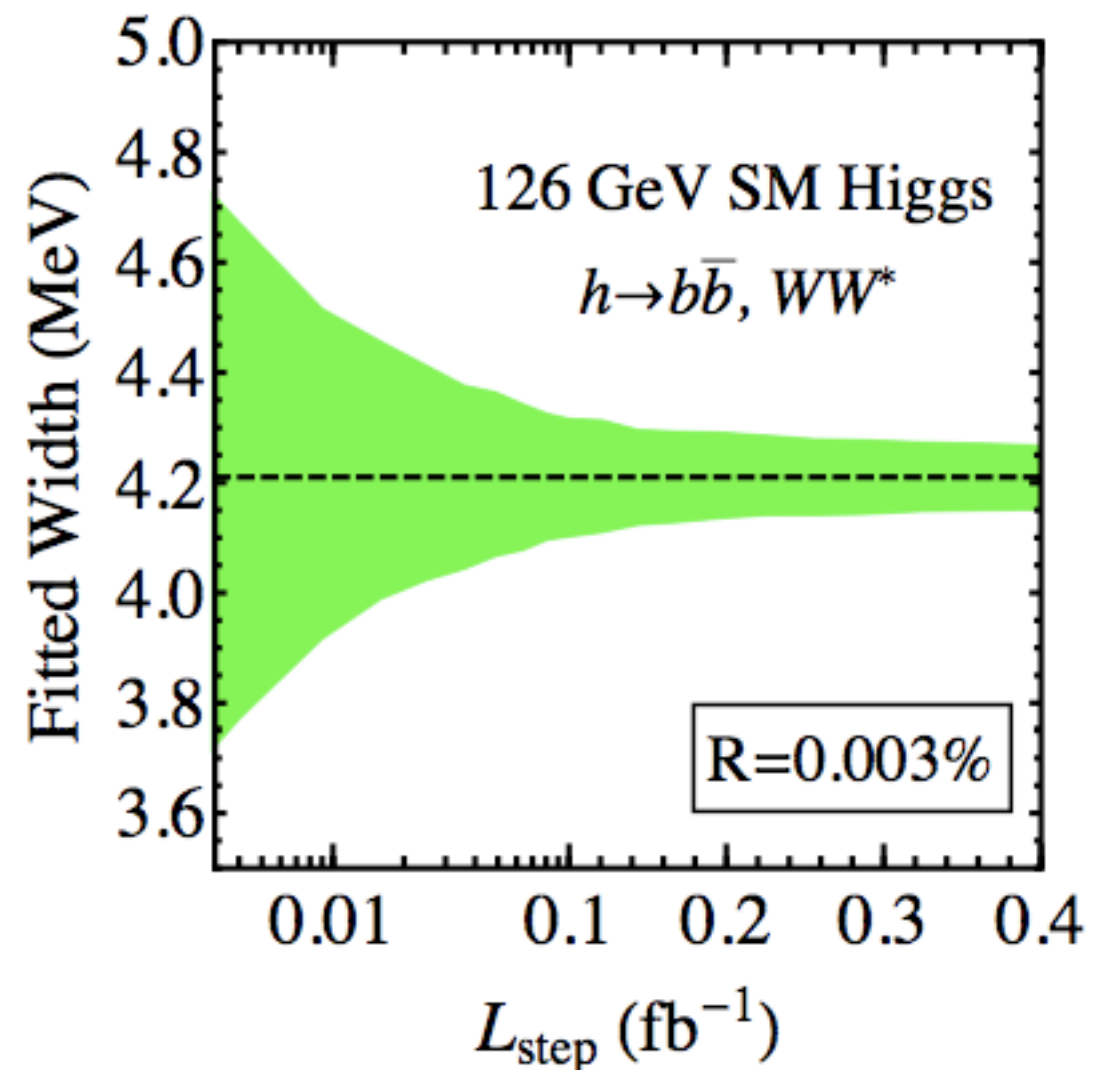
1%-10%
precision

Future muon collider

- ★ Muon collider: direct scan of Higgs threshold.
- ★ Biggest systematic uncertainty from knowledge of muon beam.



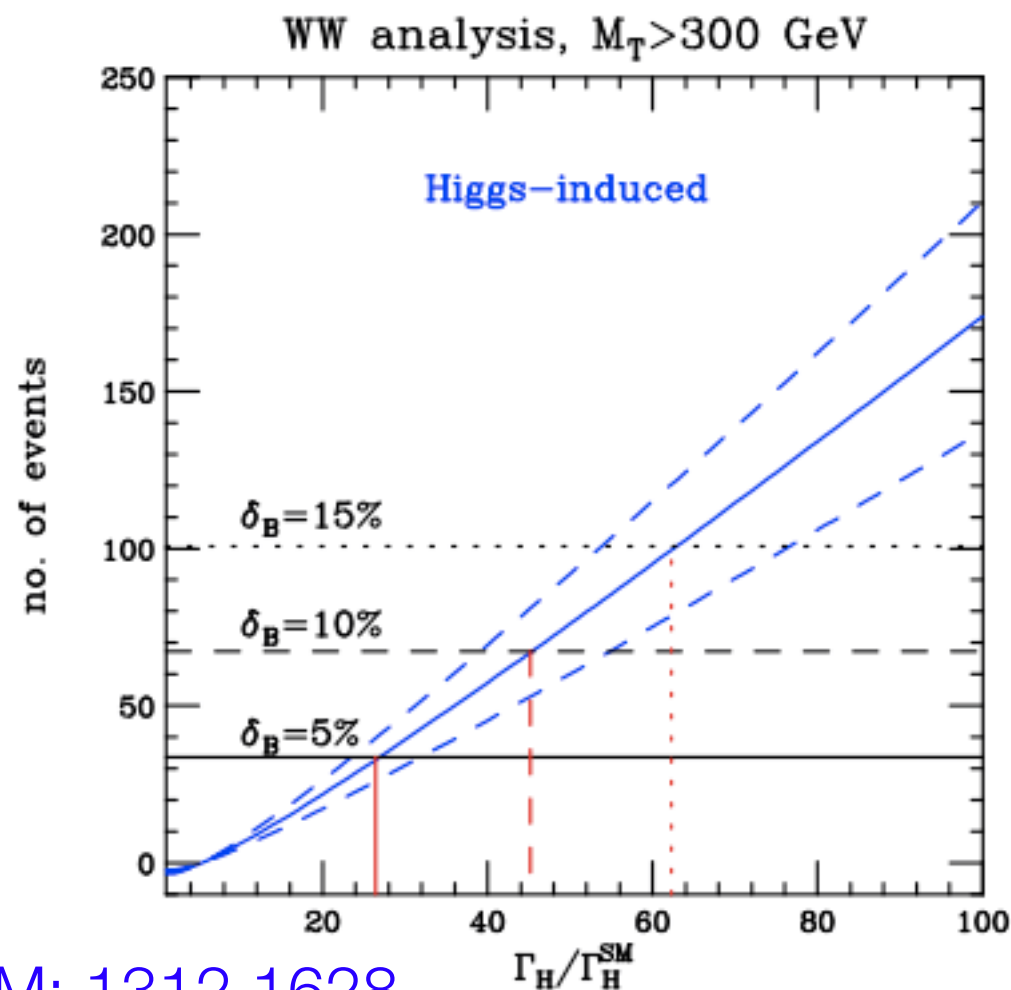
Muon collider Higgs factory
study, 1308.2143



~5% precision

Estimate of WW sensitivity

- ★ Usual cuts to isolate Higgs on-shell signal remove tail, so some cuts must be lifted.
- ★ Estimated sensitivity from ATLAS results, extrapolating uncertainties from on-shell to off-shell region.
- ★ Leap of faith: extrapolation, background estimation, systematic uncertainties, ...



- $\langle B \rangle = 336$ events
- Try to be conservative by using systematic uncertainty on theory and your choice of experimental systematic uncertainties.

$$\Gamma_H < 45^{+9}_{-7} \Gamma_H^{\text{SM}}$$

- Different flavour, 20 fb^{-1} , $\delta_B = 10\%$.